

Energy Harvesting: introduction

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Summary

- ▶ Energy harvesting applications and principles
- ▶ Fundamentals of vibration energy harvesters
- ▶ Beyond linear systems: linear and nonlinear approaches
- ▶ Conclusions

Energy harvesting applications

Wireless Sensor Networks

Structural Monitoring

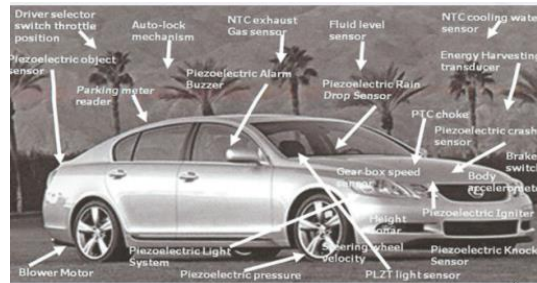


02/07/2014 - Belo Horizonte (Brazil)
(birdge collapse at FIAT factory)

Environmental Monitoring

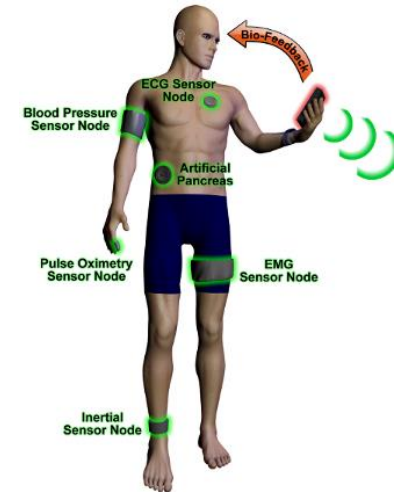


Transportation



Wearable sensing for health applications

Emergency medical response
Monitoring, pacemaker, defibrillators

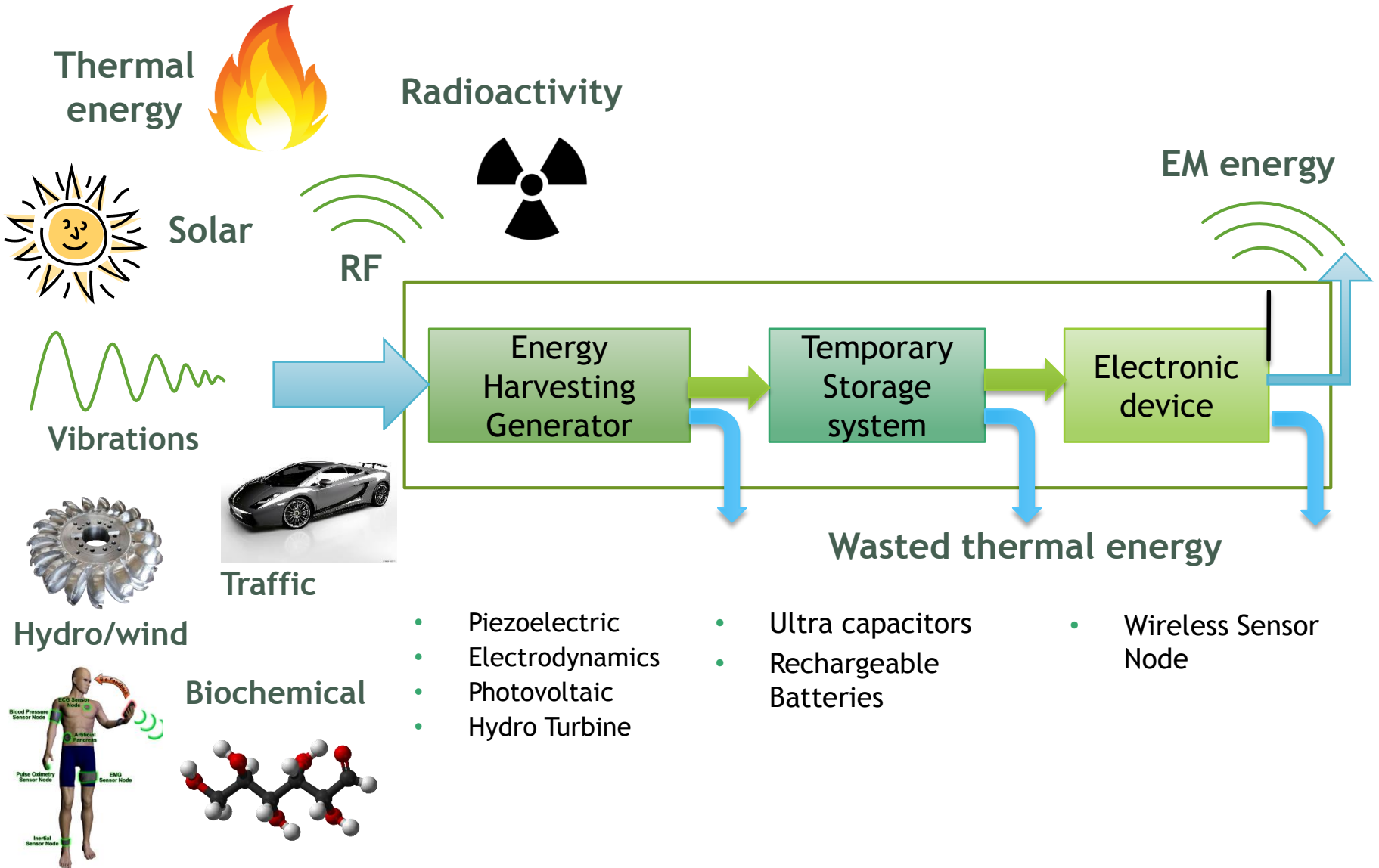


Military applications



Energy Harvesting could enable 90% of WSNs applications (IdTechex)

Power sources available from the ambient



Examples of energy harvesting systems



Tree - vegetation



Sailing ship (XVI-XVII century)

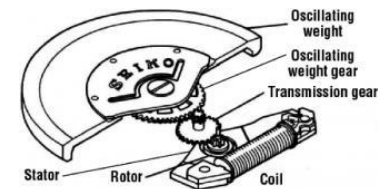


Crystal radio - 1906



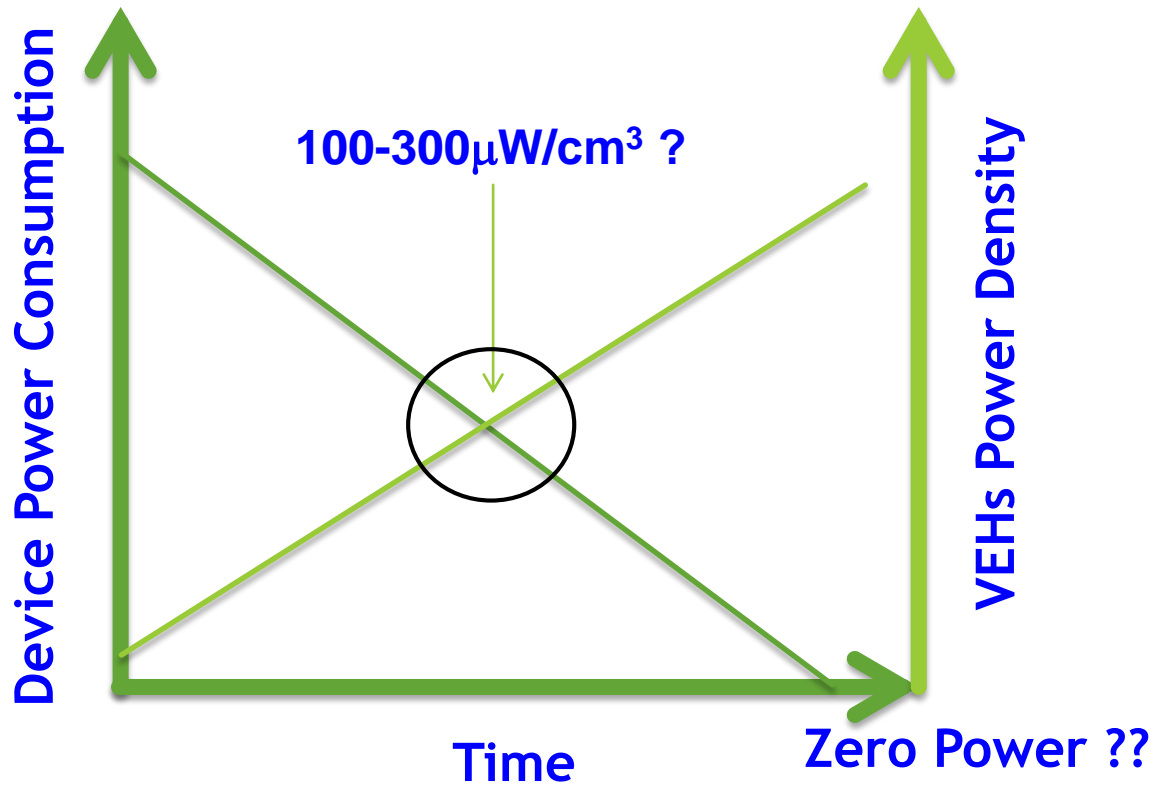
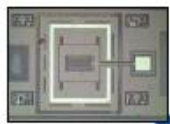
First automatic wristwatch,
Harwood, c. 1929 (Deutsches
Uhrenmuseum, Inv. 47-3543)

First automatic watch.
[Abraham-Louis Perrelet](#),
Le Locle. 1776



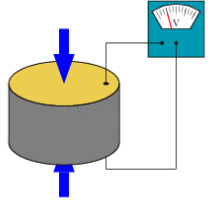
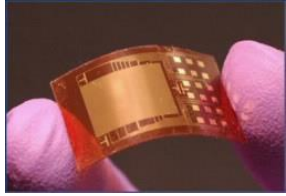
Self-charging
Seiko wristwatch

Vibration energy harvesting versus power requirements

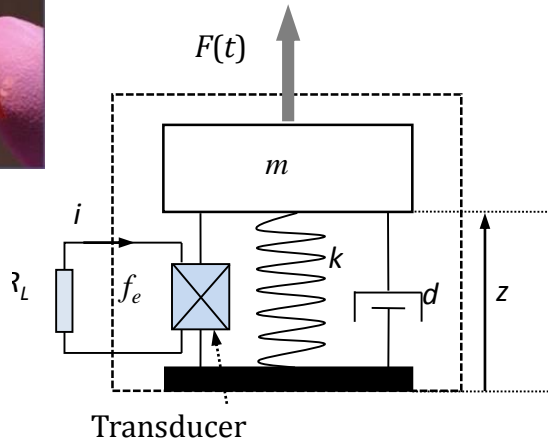


Vibration Energy Harvesters (VEHs): basics

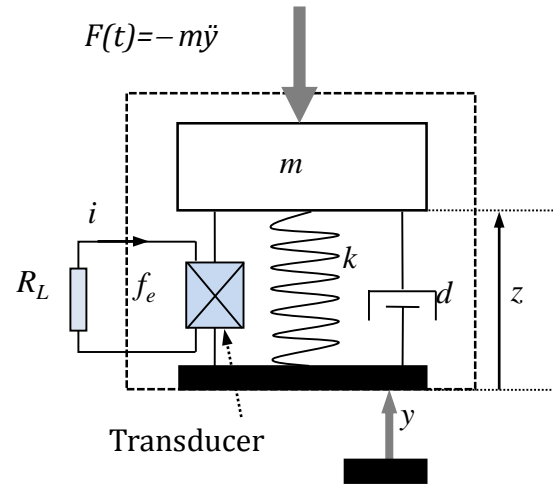
zinc oxide (ZnO) nanowires
Wang et al. 2008



Energy Harvesting from dancing



Transducer

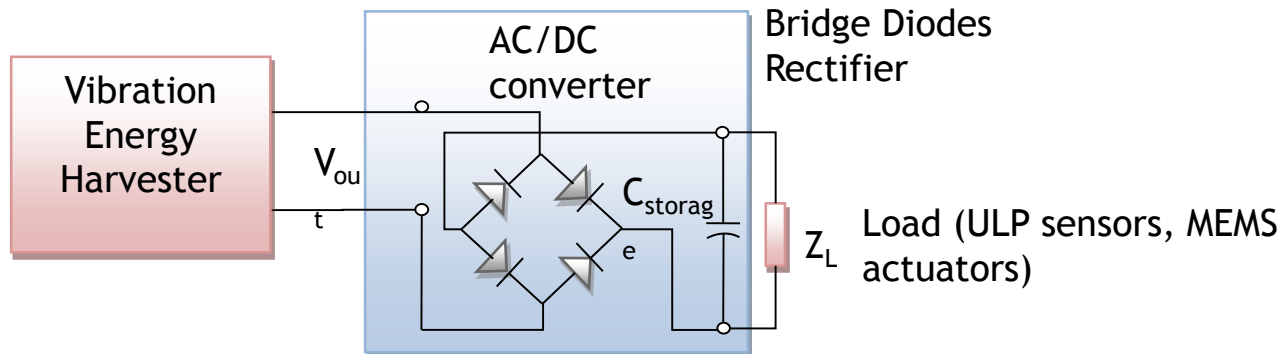


Transducer



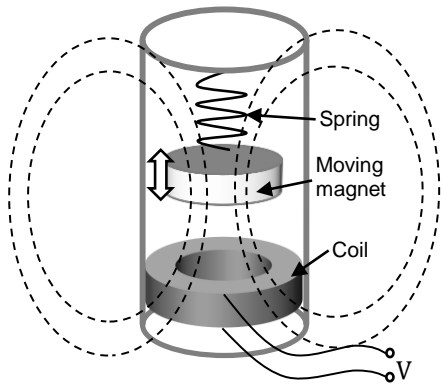
Energy harvesting from moth vibrations
Chang. MIT 2013

Inertial generators are more flexible than direct-force devices because they require only one point of attachment to a moving structure, allowing a greater degree of miniaturization.

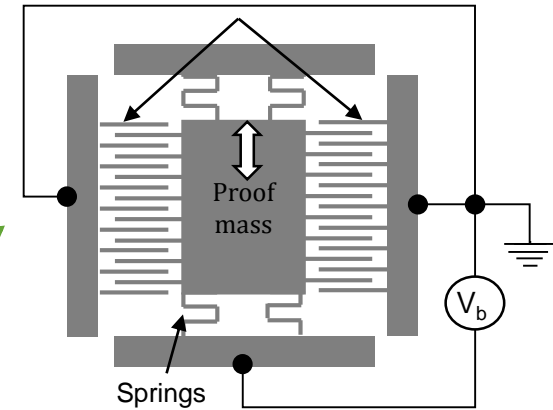


Vibration Energy Harvesters (VEHs): basics

Electromagnetic

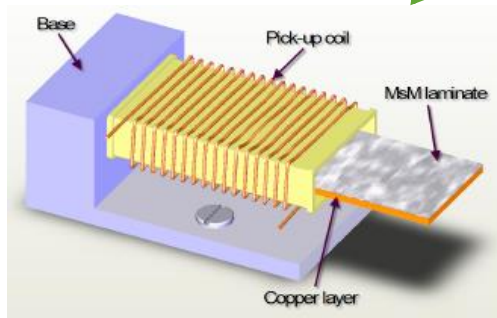


Electrostatic/Capacitive

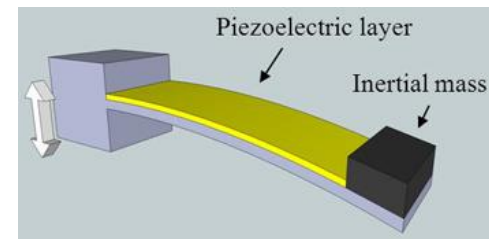


Vibration
Harvesting
Generator

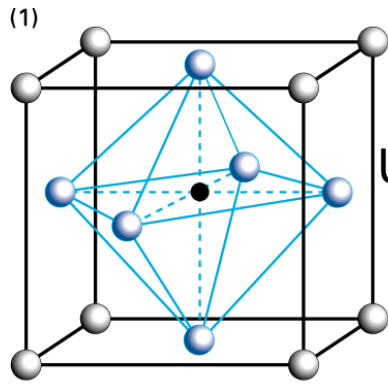
Magnetostrictive



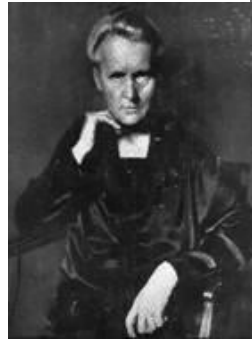
Piezoelectric



Piezoelectric conversion

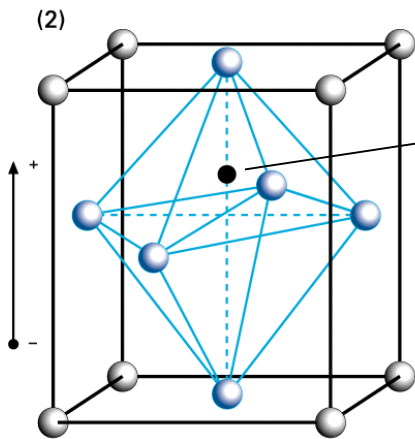


Unpolarized
Crystal

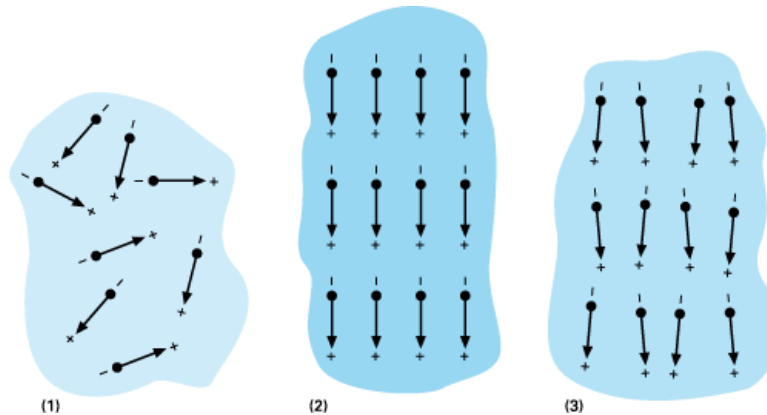
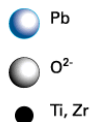


Pioneering work on the direct piezoelectric effect (stress-charge) in this material was presented by [Jacques and Pierre Curie in 1880](#)

In 1903 Pierre received the Nobel Prize in Physics with his wife, Marie Skłodowska-Curie and Henri Becquerel, for the research on the radiation phenomena discovered by Professor Henri Becquerel.



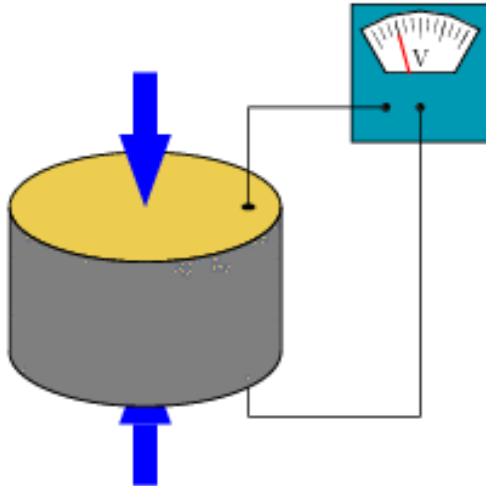
Polarized
Crystal



After poling the zirconate-titanate atoms are off center. The molecule becomes elongated and polarized

Piezoelectric conversion

Stress-to-charge conversion



direct piezoelectric effect

Biological

- Bones
- DNA !!!

Naturally-occurring crystals

- Berlinite (AlPO_4), a rare phosphate mineral that is structurally identical to quartz
- Cane sugar
- Quartz (SiO_2)
- Rochelle salt

Man-made ceramics

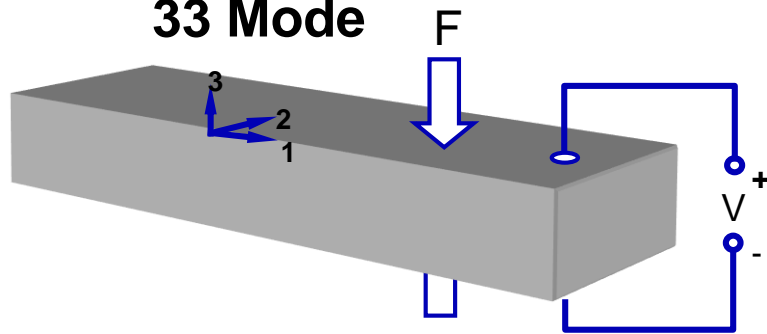
- Barium titanate (BaTiO_3)—Barium titanate was the first piezoelectric ceramic discovered.
- Lead titanate (PbTiO_3)
- Lead zirconate titanate ($\text{Pb}[\text{Zr}_x\text{Ti}_{1-x}]\text{O}_3$ $0 \leq x \leq 1$)—more commonly known as **PZT**, lead zirconate titanate is the most common piezoelectric ceramic in use today.
- Lithium niobate (LiNbO_3)

Polymers

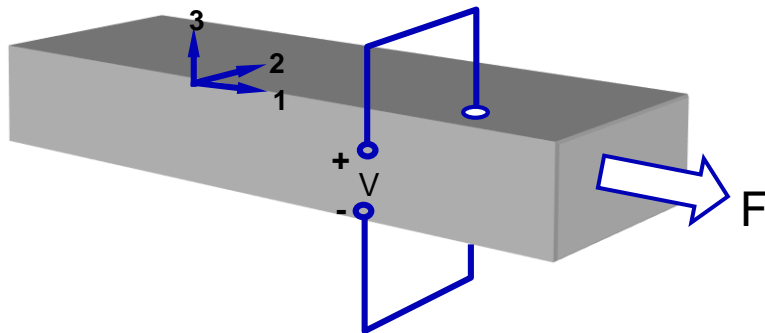
- Polyvinylidene fluoride (PVDF): exhibits piezoelectricity several times greater than quartz. Unlike ceramics, long-chain molecules attract and repel each other when an electric field is applied.

Piezoelectric conversion

33 Mode



31 Mode



$$S = [s_E]T + [d^t]E$$

$$D = [d]T + [\varepsilon_T]E$$

Strain-charge



$$T = [c^E]S - [e^t]E$$

$$D = [e]S + [\varepsilon^S]E$$

Stress-charge

- S = strain vector (6x1) in Voigt notation
- T = stress vector (6x1) [N/m²]
- s_E = compliance matrix (6x6) [m²/N]
- c^E = stiffness matrix (6x6) [N/m²]
- d = piezoelectric coupling matrix (3x6) in Strain-Charge [C/N]
- D = electrical displacement (3x1) [C/m²]
- e = piezoelectric coupling matrix (3x6) in Stress-Charge [C/m²]
- ε = electric permittivity (3x3) [F/m]
- E = electric field vector (3x1) [N/C] or [V/m]

Conversion techniques comparison

Technique	Advantages 	Drawbacks 
Piezoelectric	<ul style="list-style-type: none">• high output voltages• well adapted for miniaturization• high coupling in single crystal• no external voltage source needed	<ul style="list-style-type: none">• expensive• small coupling for piezoelectric thin films• large load optimal impedance required ($M\Omega$)• Fatigue effect
Electrostatic	<ul style="list-style-type: none">• suited for MEMS integration• good output voltage (2-10V)• possibility of tuning electromechanical coupling• Long-lasting	<ul style="list-style-type: none">• need of external bias voltage• relatively low power density at small scale
Electromagnetic	<ul style="list-style-type: none">• good for low frequencies (5-100Hz)• no external voltage source needed• suitable to drive low impedances	<ul style="list-style-type: none">• inefficient at MEMS scales: low magnetic field, micro-magnets manufacturing issues• large mass displacement required.

Example of vibration sources

Human activity

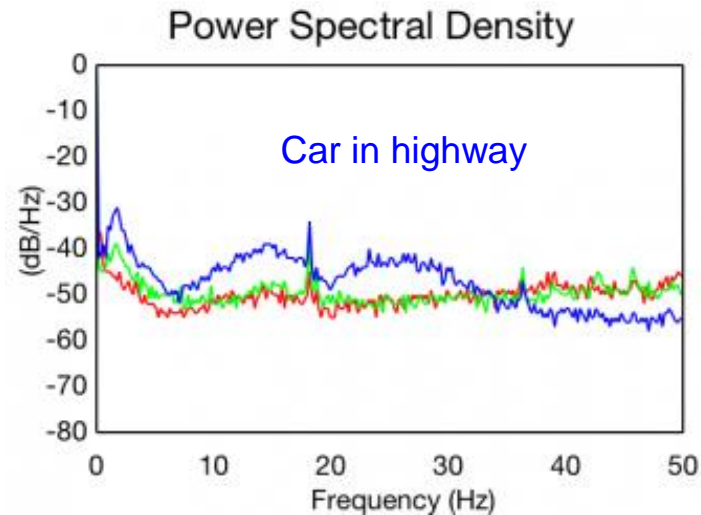
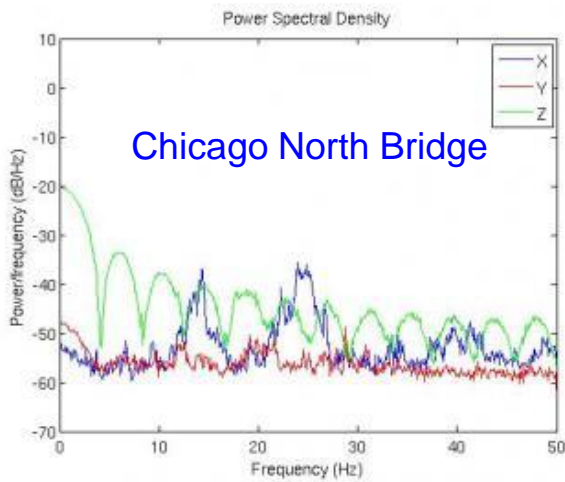
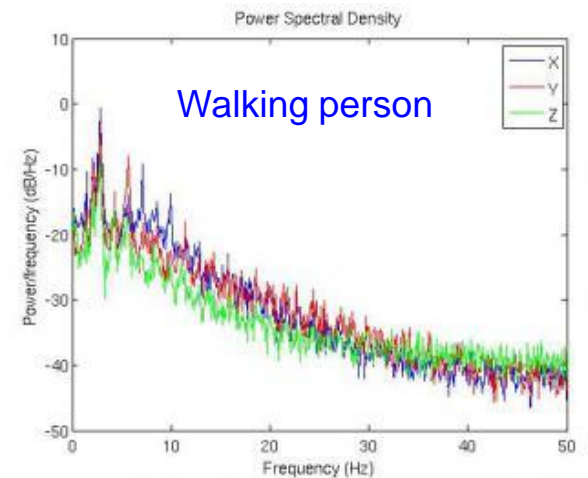
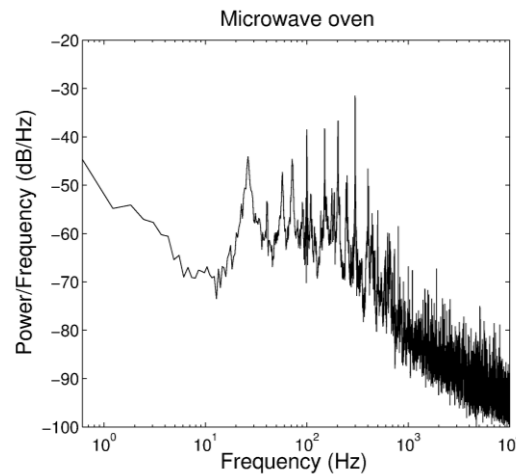
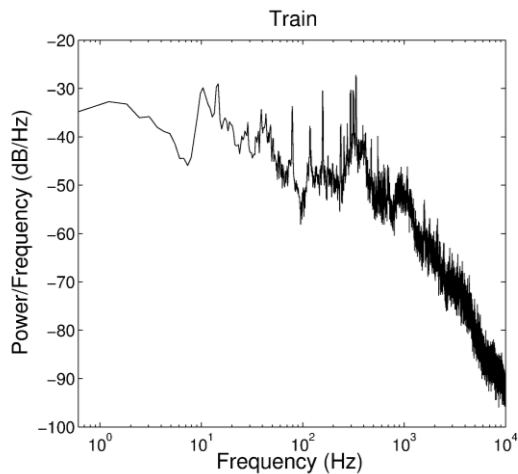
Scenario	\bar{P}
Taking a book off a shelf	$<10 \mu\text{W}$
Putting on reading glasses	$<10 \mu\text{W}$
Reading a book	$<10 \mu\text{W}$
Writing with a pencil	$10\text{--}15 \mu\text{W}$
Opening a drawer	$10\text{--}30 \mu\text{W}$
Spinning in a swivel chair	$<10 \mu\text{W}$
Opening a building door	$<1 \mu\text{W}$
Shaking an object	$>3,000 \mu\text{W}$

Activity	Sensing unit placement	# subjects	Median f_m (Hz)	\bar{P} (μW)			Median r (Kb/s)
				25 th percentile	Median	75 th percentile	
Relaxing	Trouser pocket	42	1.9		3.1	4.8	0.6
	Waist belt	42	2.0		2.4	4.8	0.5
	Trouser pocket	42	2.0		1.4	5.9	0.3
Walking	Shirt pocket	42	1.9		155.2	186.0	31.0
	Waist belt	42	2.0		180.3	202.4	36.0
	Trouser pocket	42	2.0		202.4	813.3	40.4
Running	Shirt pocket	42	2.8		813.3	910.0	162.6
	Waist belt	41	2.8		678.3	752.8	135.6
	Trouser pocket	42	2.8		612.7	678.3	122.5
Cycling	Shirt pocket	30	3.5		52.0	59.2	10.4
	Waist belt	29	3.8		45.4	59.2	9.1
	Trouser pocket	30	1.1		41.3	59.5	8.3

Gorlatova, M et al (2013). Movers and shakers: Kinetic energy harvesters for the internet of things.

3.5
3.8
1.1

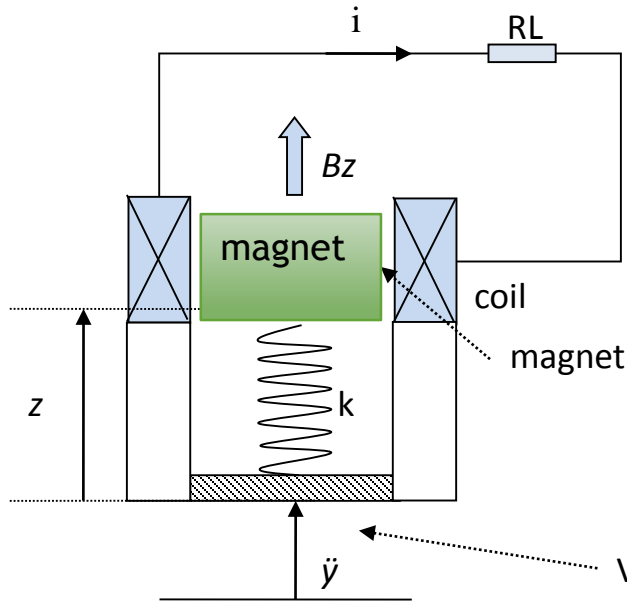
Example of vibration sources



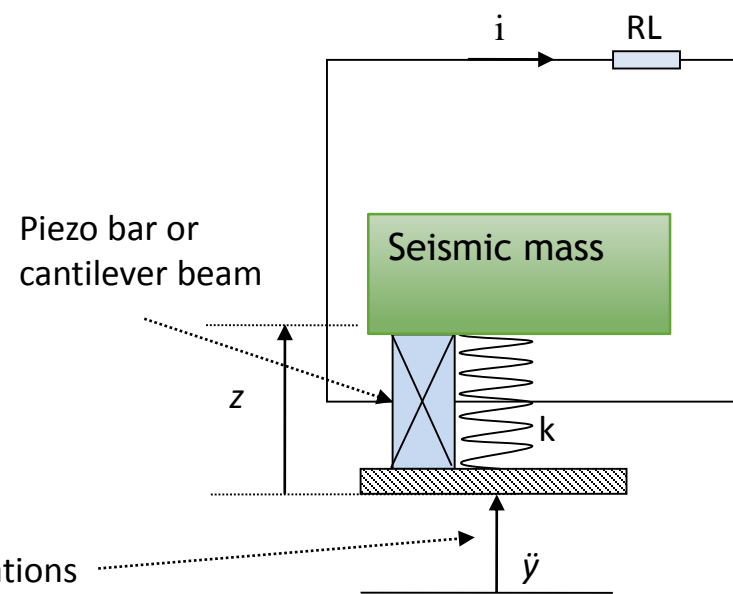
<http://realvibration.nipslab.org>

A general model for VEHs

Electromagnetic transduction



Piezoelectric transduction



$$\begin{cases} m\ddot{z} + d\dot{z} + \frac{dU(z)}{dz} + \alpha V_L = -m\ddot{y} \\ \dot{V}_L + (\omega_c + \omega_i)V_L = \lambda\omega_c\dot{z} \end{cases}$$

A general model for VEHs

LINEAR mechanical oscillator

$$U(z) = \frac{1}{2}kz^2 \quad \rightarrow$$

$$\begin{cases} m\ddot{z} + d\dot{z} + kz + \alpha V_L = -m\ddot{y} \\ \dot{V}_L + (\omega_c + \omega_i)V_L = \lambda\omega_c \dot{z} \end{cases}$$

Laplace transform

$$\ddot{y} = Y_0 e^{j\omega t} \quad \rightarrow \quad \begin{pmatrix} ms^2 + ds + k & \alpha \\ -\lambda\omega_c s & s + \omega_c \end{pmatrix} \begin{pmatrix} Z \\ V \end{pmatrix} = \begin{pmatrix} -mY \\ 0 \end{pmatrix}$$

$$Z = \frac{-mY}{\det A} (s + \omega_c) = \frac{-mY \cdot (s + \omega_c)}{ms^3 + (m\omega_c + d)s^2 + (k + \alpha\lambda\omega_c + d\omega_c)s + k\omega_c},$$



$$V = \frac{-mY}{\det A} \lambda\omega_c s = \frac{-mY \cdot \lambda\omega_c s}{ms^3 + (m\omega_c + d)s^2 + (k + \alpha\lambda\omega_c + d\omega_c)s + k\omega_c}.$$

Hence, the transfer functions between displacement and voltage over input acceleration are given by

$$H_{zv}(s) = \frac{Z}{Y}, \quad (a)$$

$$H_{vr}(s) = \frac{V}{Y}. \quad (b)$$

By substituting $s=j\omega$ in , we can calculate the electrical power dissipated across the resistive load



$$P_e(\omega) = \frac{Y_0^2}{2R_L} \left| \frac{m_2 \lambda \omega_c j \omega}{(\omega_c + j\omega)(-m_2 \omega^2 + d_2 j\omega + k_2) + \alpha \lambda \omega_c j \omega} \right|^2$$

Piezoelectric conversion

Strain-charge

$$\mathbf{S} = \mathbf{s}_E \cdot \mathbf{T} + \mathbf{d}^t \cdot \mathbf{E}$$

$$\mathbf{D} = \mathbf{d} \cdot \mathbf{T} + \boldsymbol{\varepsilon}_T \cdot \mathbf{E}$$

Stress-charge

$$\mathbf{T} = \mathbf{c}_E \cdot \mathbf{S} - \mathbf{e}^t \cdot \mathbf{E}$$

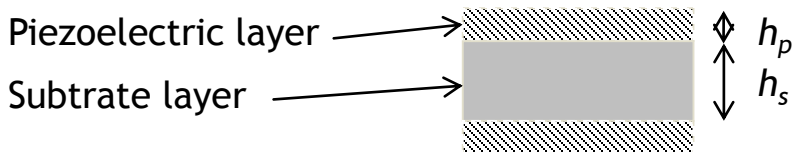
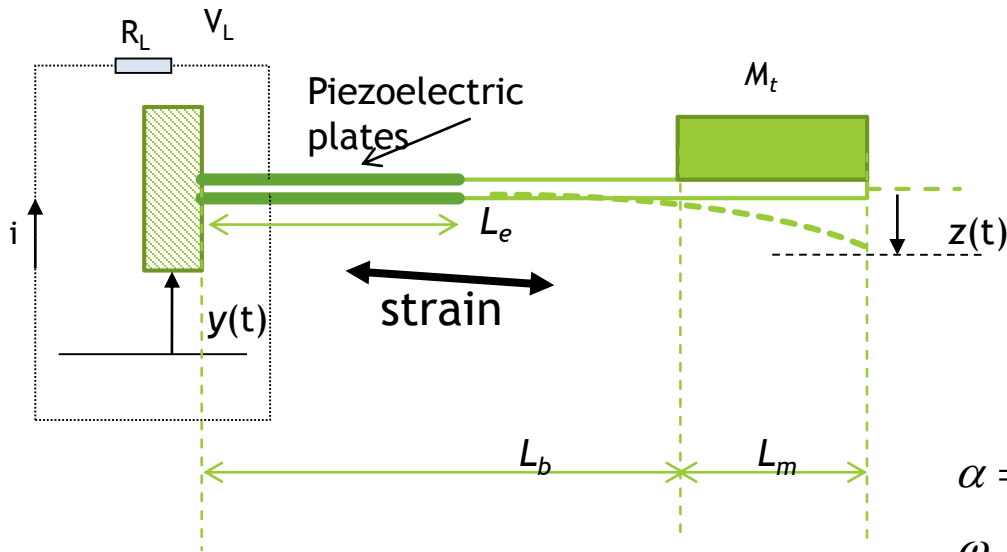
$$\mathbf{D} = \mathbf{e} \cdot \mathbf{S} + \boldsymbol{\varepsilon}_S \cdot \mathbf{E}$$

Characteristic	PZT-5H	BaTiO3	PVDF	AlN (thin film)
d_{33} (10^{-10} C/N)	593	149	-33	5,1
d_{31} (10^{-10} C/N)	-274	78	23	-3,41
k_{33}	0,75	0,48	0,15	0,3
k_{31}	0,39	0,21	0,12	0,23
ε_r	3400	1700	12	10,5

$$k_{31}^2 = \frac{\text{El.energy}}{\text{Mech.energy}} = \frac{d_{31}^2}{s_{11}^E \varepsilon_{33}^T}$$

Electromechanical Coupling is an adimensional factor that provides the effectiveness of a piezoelectric material. IT's defined as the ratio between the mechanical energy converted and the electric energy input or the electric energy converted per mechanical energy input

Piezoelectric conversion



E_p and E_s are the Young's modulus of piezo layer and steel substrate respectively

$$\begin{cases} m\ddot{z} + d\dot{z} + kz + \alpha V_L = -m\ddot{y} \\ \dot{V}_L + (\omega_c + \omega_i)V_L = \lambda\omega_c \dot{z} \end{cases}$$

$$\alpha = kd_{31} / h_p k_2,$$

$$\lambda = \alpha R_L,$$

$$\omega_c = 1 / R_L C_p,$$

$$\omega_i = 1 / R_i C_p,$$

$$k = k_1 k_2 E_p,$$

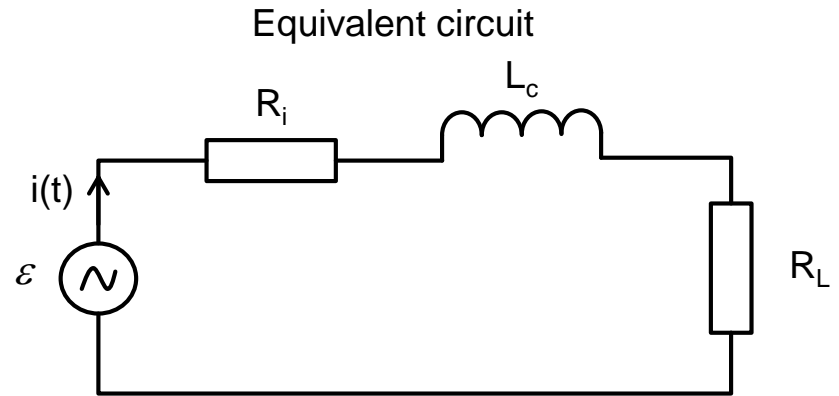
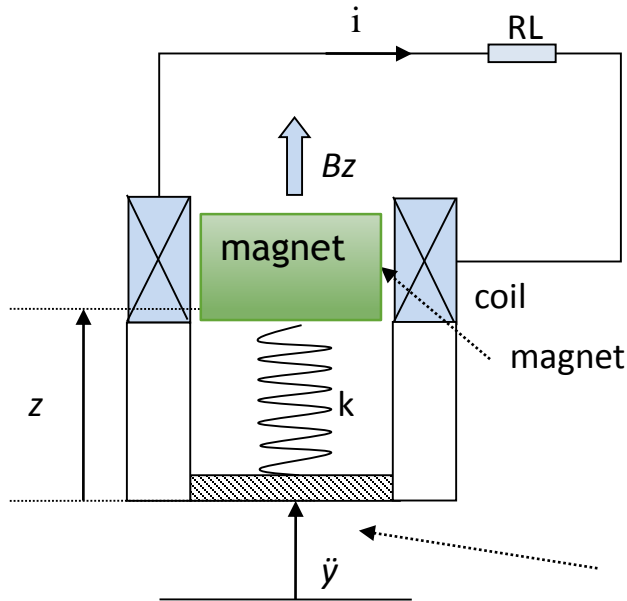
$$k_1 = \frac{2I}{b(2l_b + l_m - l_e)},$$

$$k_2 = \frac{3b(2l_b + l_m - l_e)}{l_b^2 \left(2l_b + \frac{3}{2}l_m \right)},$$

$$b = \frac{h_s + h_p}{2},$$

$$I = 2 \left[\frac{w_b h_p^3}{12} + w_b h_p b^2 \right] + \frac{E_s / E_p w_b h_s^3}{12},$$

Electromagnetic conversion



$$\begin{cases} m\ddot{z} + d\dot{z} + kz + \alpha V_L = -m\ddot{y} \\ \dot{V}_L + (\omega_c + \omega_i)V_L = \lambda\omega_c \dot{z} \end{cases}$$

$$\alpha = Bl / R_L,$$

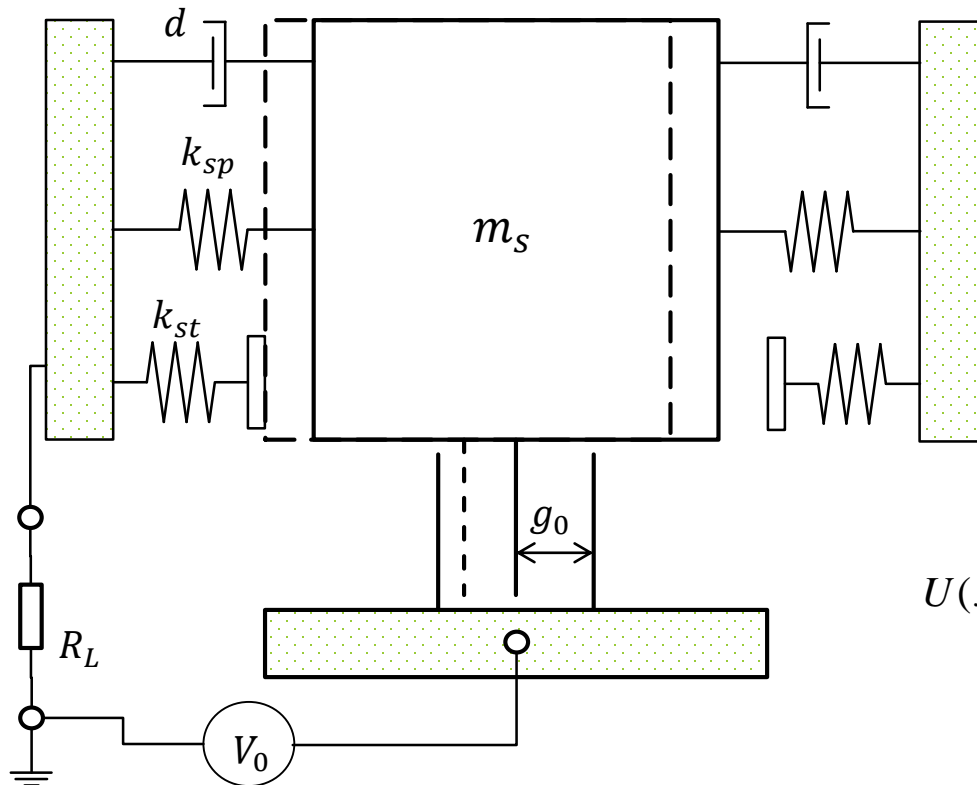
$$\omega_c = R_L / L_c,$$

$$\lambda = Bl = \alpha R_L,$$

$$\omega_i = R_i / L_c,$$

MEMS electrostatic kinetic energy harvester

Mathematical modeling



Governing equations

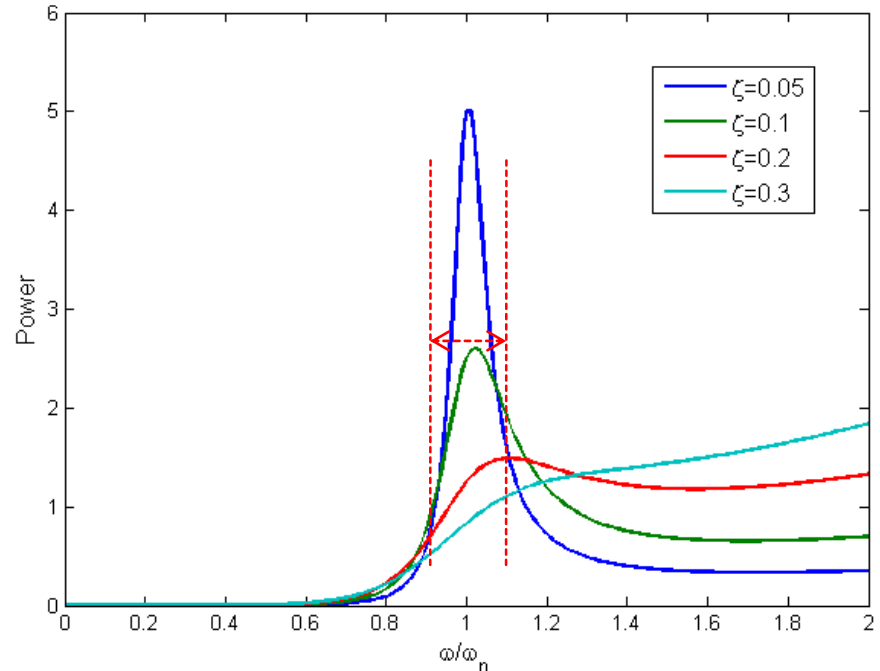
$$m \frac{d^2 x}{dt^2} + (c_a + c_i) \frac{dx}{dt} + \frac{dU(x)}{dx} = -m \frac{d^2 y}{dt^2},$$

$$R_L \frac{d}{dt} (C \cdot V) + V = U_0,$$

$$U(x) = \begin{cases} \frac{1}{2} k_{sp} x^2 - \frac{1}{2} C(x) U_0^2, & \text{for } |x| < x_{lim} \\ \frac{1}{2} (k_{sp} + k_{st}) x^2 - \frac{1}{2} C(x) U_0^2, & \text{for } |x| \geq x_{lim} \end{cases}$$

Main limits of resonant VEHS

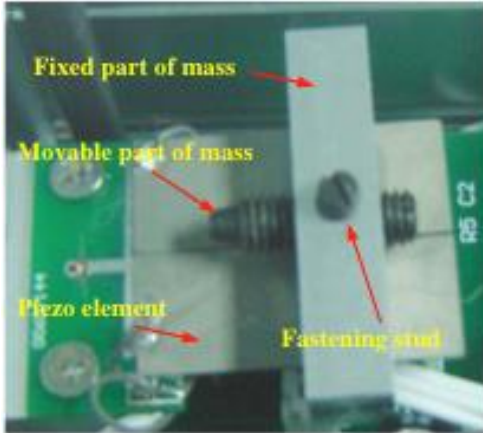
- narrow bandwidth that implies constrained resonant frequency-tuned applications
- Non-adaptation to variable vibration sources
- small inertial mass and high resonant frequency at micro/nano-scale -> most of vibration sources are below 100 Hz



At 20% off the resonance
the power falls by 80-90%

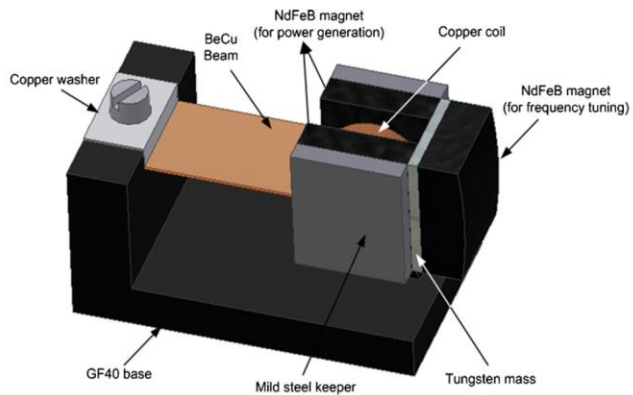
Beyond linear harvesting systems

Frequency tuning

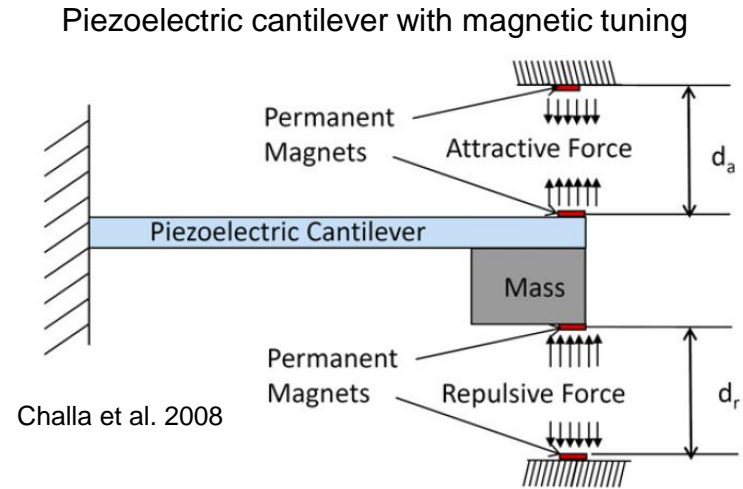


Piezoelectric cantilever with a movable mass

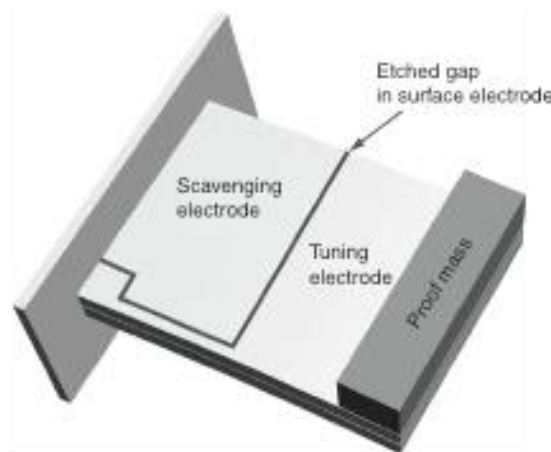
Wu et al. 2008



Zhu, et al. (2010). *Sensors and Actuators A: Physical*



Challa et al. 2008



Piezoelectric beam with a scavenging and a tuning part

Roundy and Zhang 2004

Beyond linear harvesting systems

Frequency tuning

Table 2. Summary of the reported resonance tuning methods.

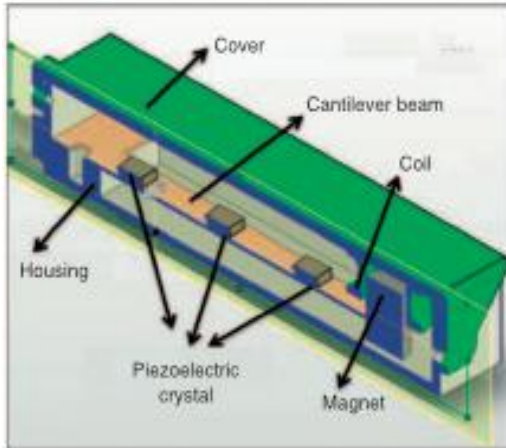
Author	Methods	Tuning range (Hz)	Tunability, $\left(\frac{\text{frequency change}}{\text{average frequency}}\right)$ (%)	Tuning load (force, distance, and voltage)	Energy or power for tuning	Automatic controller
Leland and Wright (2006)	Mechanical (passive)	200–250 (7.1 g tip mass)	22.22	Up to 65 N	–	×
Eichhorn et al. (2008)	Mechanical (passive)	292–380	26.19	Up to 22.75 N	–	×
Hu et al. (2007)	Mechanical (passive)	58.1–169.4	97.85	–50–50 N	–	×
Morris et al. (2008)	Mechanical (passive)	80–235 (can be wider)	≥ 98.41	≈ 1.25 mm	–	×
Loverich et al. (2008)	Mechanical (passive)	56–62	10.17	0.5 mm	–	×
Wu et al. (2008)	Mechanical (passive)	130–180	32.26	21 mm	–	×
Challa et al. (2008)	Magnetic (passive)	22–32	37.04	3 cm	85 mJ	×
Reissman et al. (2009)	Magnetic (passive)	88–99.38	12.15	1.5 cm	–	×
Zhu et al. (2008)	Magnetic (passive)	67.6–98	36.71	3.8 mm	2.04 mJ/mm	✓
Wu et al. (2006)	Piezoelectric (active)	91.5–94.5	3.23	–	μ W level (for controller)	✓
Peters et al. (2009)	Piezoelectric (active)	66–89 (actuator PL140)	29.68	± 5 V	150 mW (discrete control circuit)	✓
Roundy and Zhang (2005)	Piezoelectric (active)	64.5–67	3.80	5 V	440 μ W	×
Wischke et al. (2010)	Piezoelectric (semi-passive)	20 (10 mm long electrode)	≈ 6.7	–65 to +130 V	200 μ J	×

Tang et al. 2010

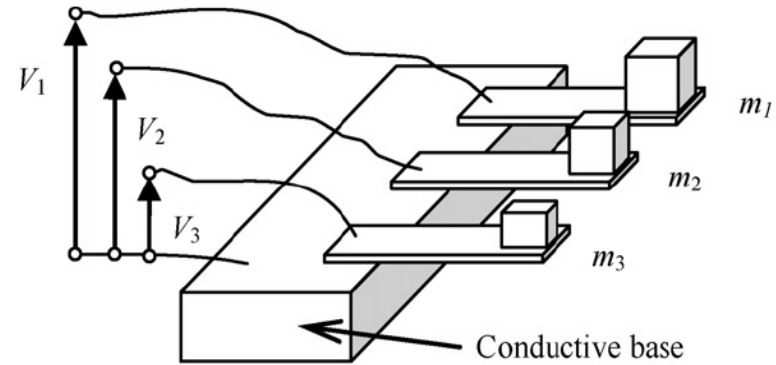
Beyond linear harvesting systems

Multimodal Energy Harvesting

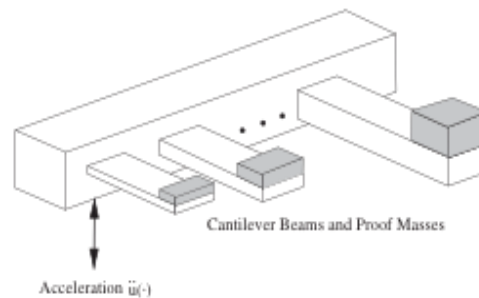
Tadesse et al. 2009



Hybrid harvester with piezoelectric and electromagnetic transduction mechanisms



Ferrari, M., et al. (2008). *Sensors and Actuators A: Physical*

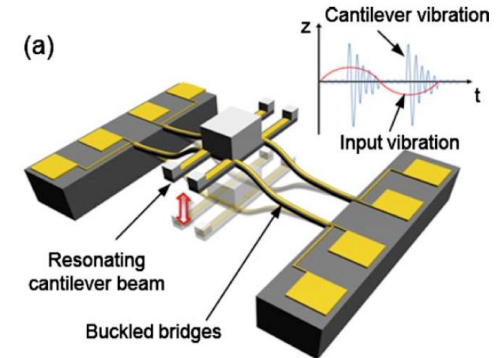
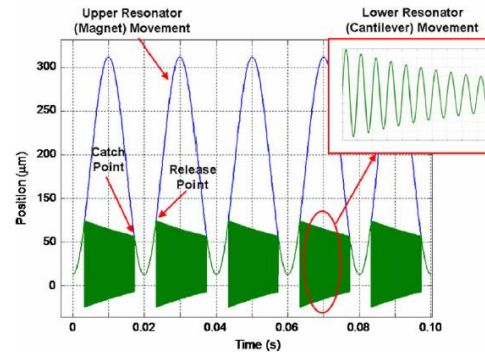
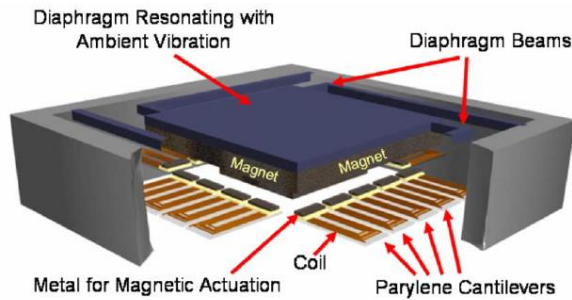


Piezoelectric cantilever arrays with various lengths and tip masses

Shahruz 2006

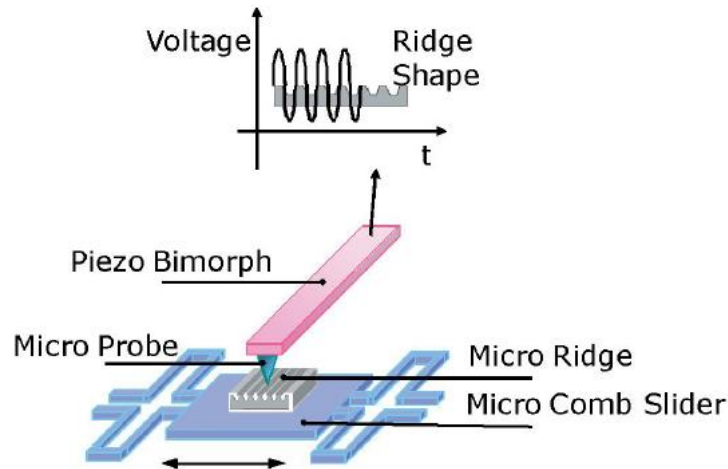
Beyond linear harvesting systems

Frequency-up conversion



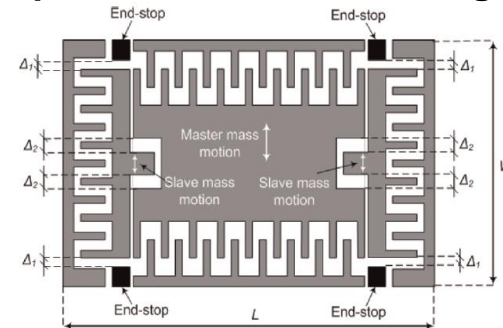
H. Kulah and K. Najafi, *IEEE Sensors Journal* **8** (3), 261 (2008).

Jung, S.-M. et al. (2010). *Applied Physics Letters*



D.G. Lee et al. *IEEE Proc.* (2007)

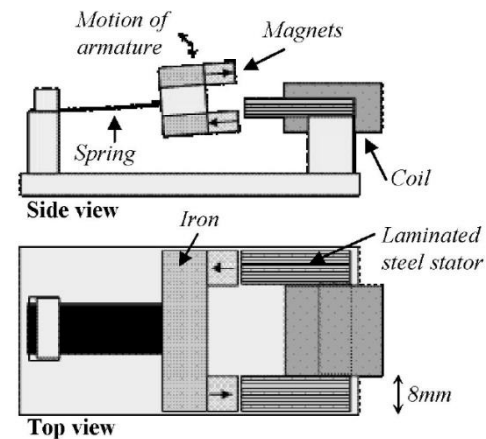
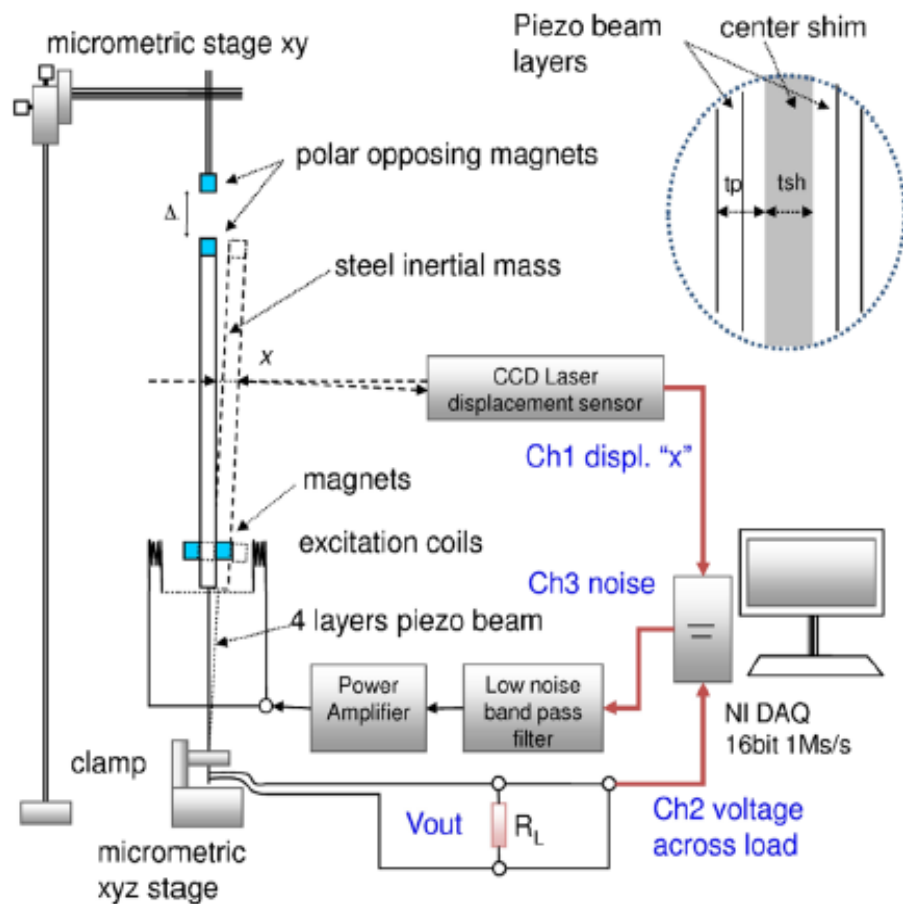
Impact electrostatic MEMS generator



Le, C. P., Halvorsen (2012). *Journal of Intelligent Material Systems and Structures*

Beyond linear harvesting systems

Nonlinear systems



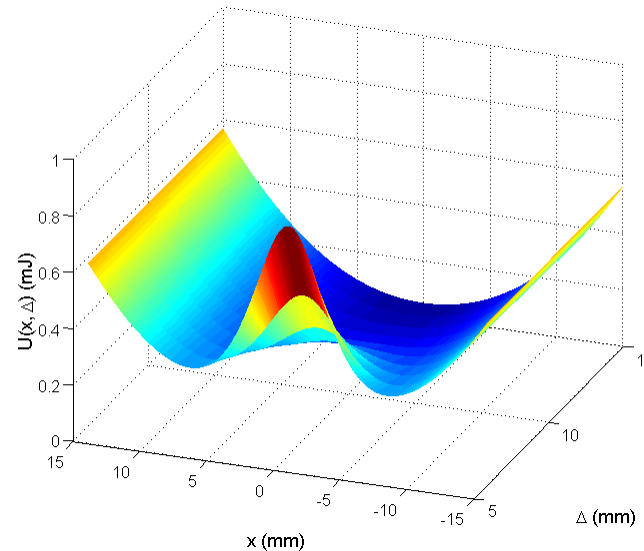
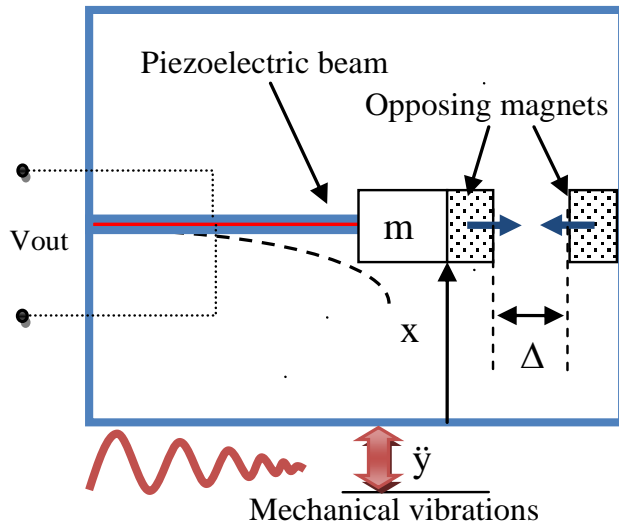
Burrow, S.G and Clare, L.R. IEEE proc. (2007)

Cottone, F., H. Vocca & L. Gammaitoni, Nonlinear Energy Harvesting. *PRL*, 102 (2009).

NiPS Summer School 2015 – July 7-12th -Fiuggi (Italy) – F. Cottone

Beyond linear harvesting systems

Nonlinear systems for vibration energy harvesting



Magneto-elastic potential

$$U(x, \Delta) = \frac{1}{2} K_{eff} x^2 + \frac{\mu_0}{2\pi} \frac{M_1 M_2}{(x^2 + \Delta^2)^{3/2}}$$

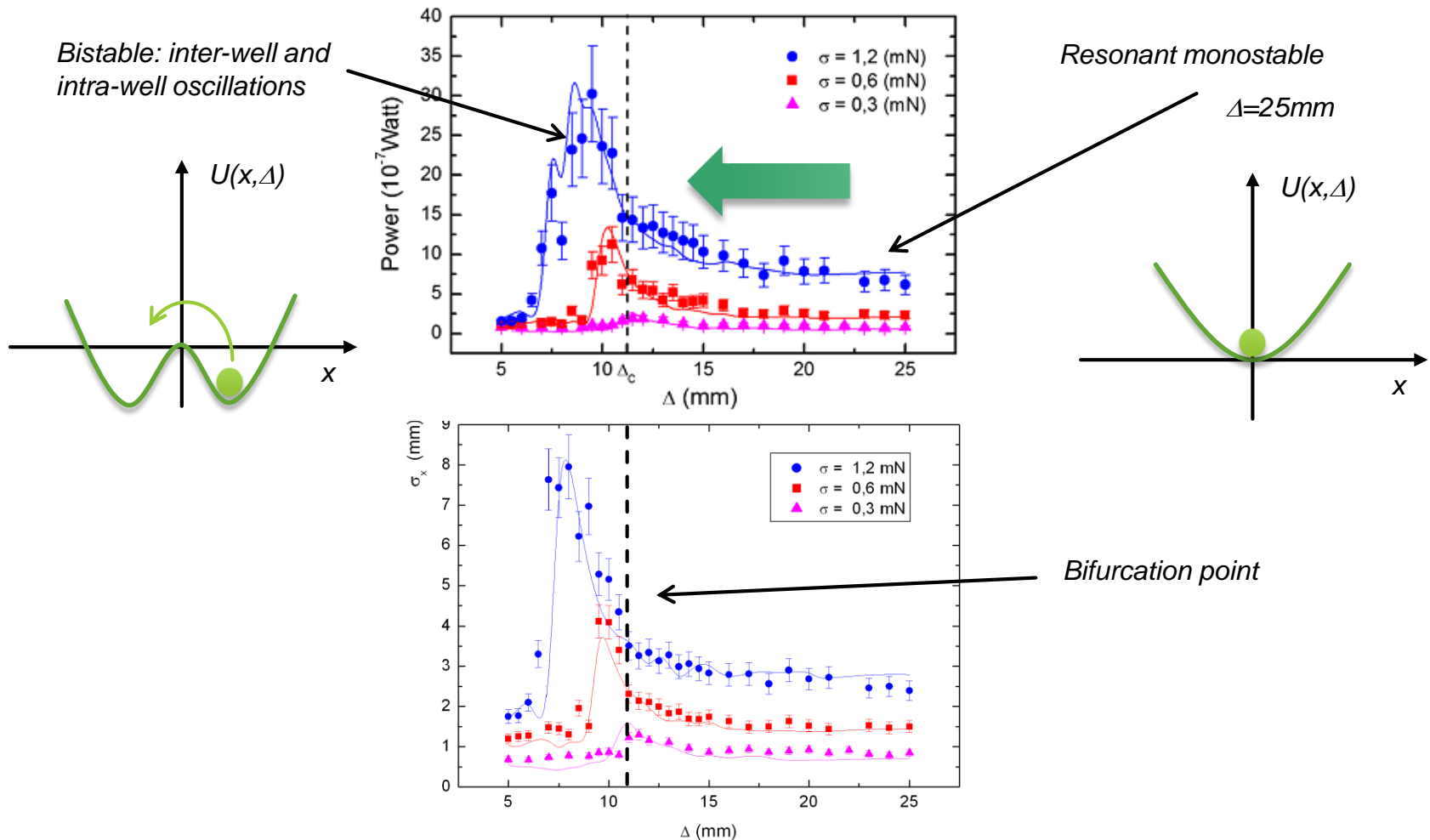
Governing equations of a single-DOF piezo-magnetoelastic model

$$\begin{cases} m\ddot{x}(t) + \delta\dot{x}(t) + K_{eff}x(t) + \frac{\partial U(x, \Delta)}{\partial x} + K_v V(t) = -m\ddot{y}(t) \\ \dot{V}(t) + \frac{1}{\tau} V(t) = K_c \dot{x}(t); & \tau = R_L C_p \end{cases}$$

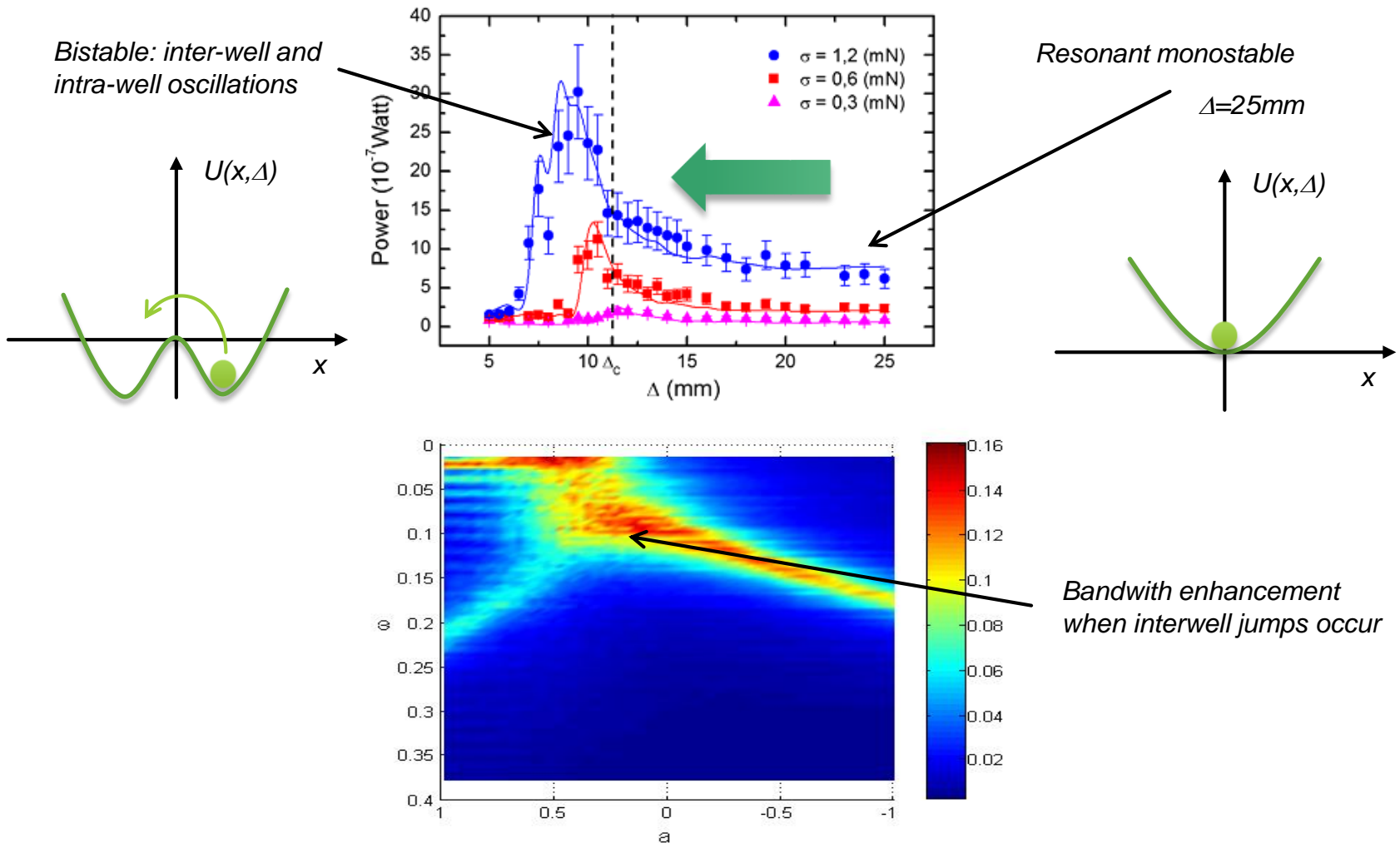
Cottone, F., H. Vocca & L. Gammaitoni. *PRL*, 102 (2009).

NiPS Summer School 2015 – July 7-12th -Fiuggi (Italy) – F. Cottone

Bistable oscillators for vibration energy harvesting



Bistable oscillators for vibration energy harvesting

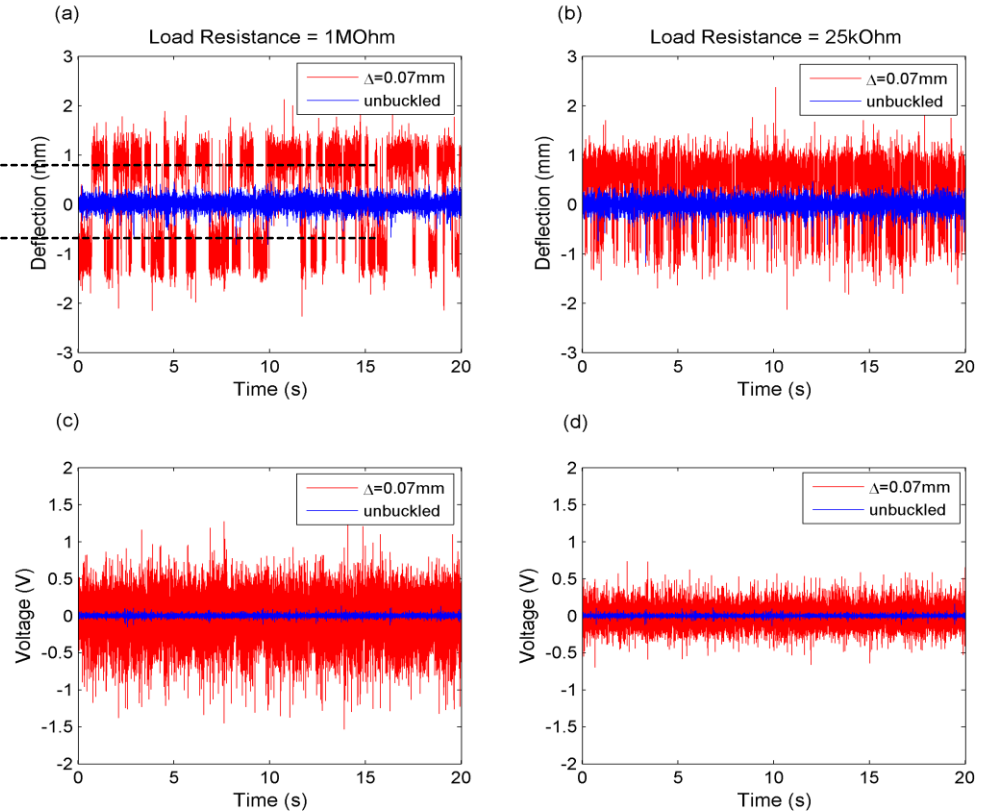
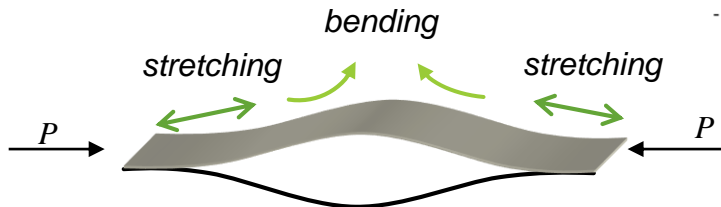
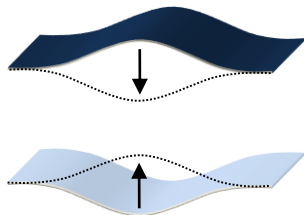


Bistable oscillators for vibration energy harvesting

Buckled beam piezoelectric harvesters

Cottone, F., Gammaitoni, L., Vocca, H., Ferrari, M., & Ferrari, V. (2012). *Smart materials and structures*, 21(3), 035021

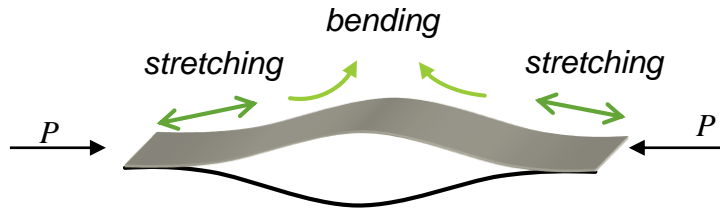
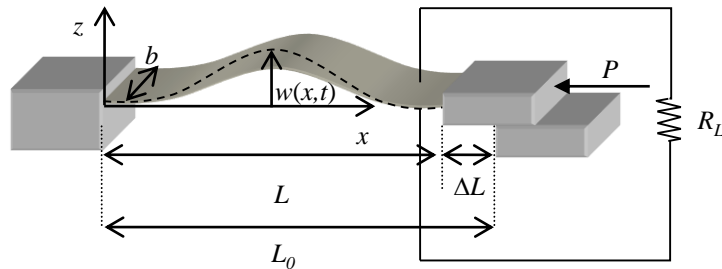
Snapping between buckled states



Bistable oscillators for vibration energy harvesting

Buckled piezoelectric beams

$$w(x, t) = w_1(x) + v(x, t)$$

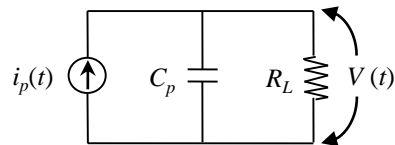
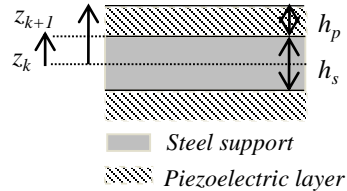


the initial buckling shape function is

$$\psi(x) = h_0(1 - \cos(2\pi x / L)) / 2$$

by applying Euler-Lagrange equations

$$\frac{d}{dt} \left(\frac{\partial \mathcal{L}}{\partial \dot{q}} \right) - \frac{\partial \mathcal{L}}{\partial q} = F(t), \quad \frac{d}{dt} \left(\frac{\partial \mathcal{L}}{\partial \dot{\lambda}} \right) - \frac{\partial \mathcal{L}}{\partial \lambda} = I(t)$$



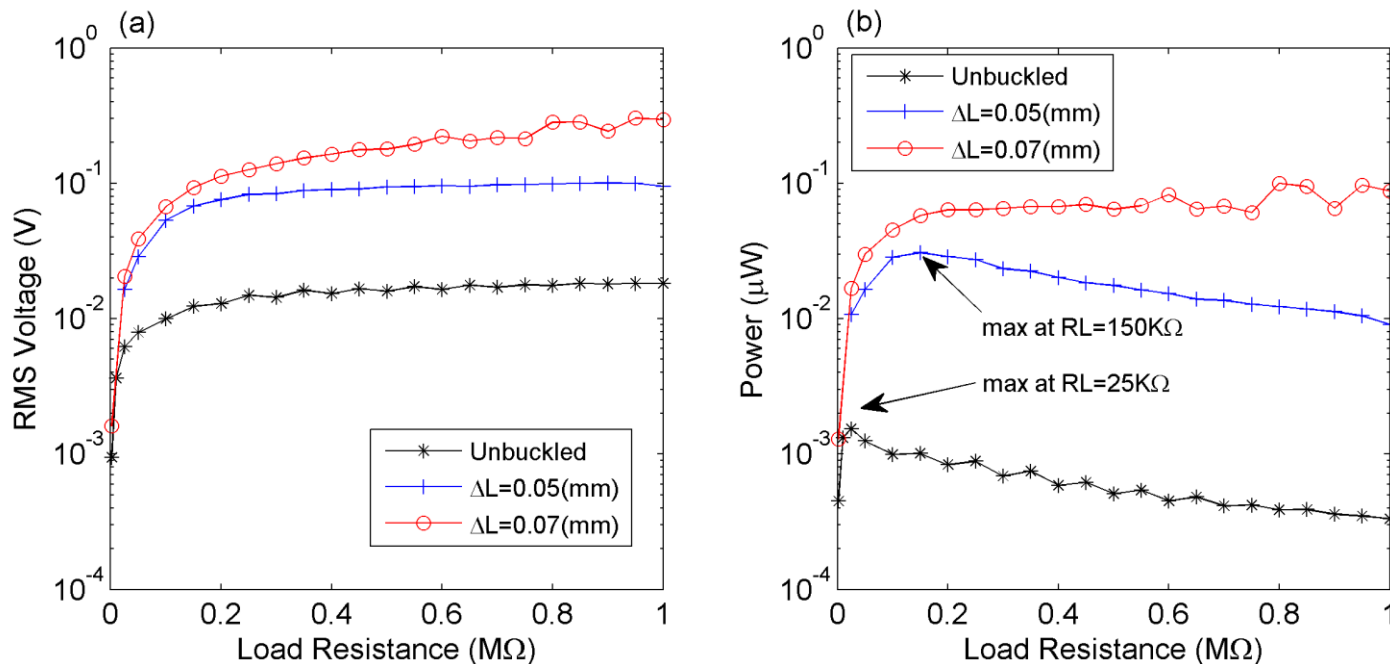
gives two coupled second order nonlinear differential equations governing the motion of the piezoelectric buckled beam

Where the output voltage is related to the flux linkage $V = -\dot{\lambda}$

$$\begin{cases} m\ddot{q} + c\dot{q} + k_3q^3 + (k_2(-k_1V)q) + k_0V = -\eta\ddot{z}, \\ \ddot{V} + \frac{2}{R_L C_p}V = 2\frac{k_0}{C_p}\dot{q} - 2\frac{k_1}{C_p}q\dot{q}. \end{cases}$$

Bistable oscillators for vibration energy harvesting

Experimental and numerical results



Cottone, F., L. Gammaitoni, H. Vocca, M. Ferrari & V. Ferrari (2012) Smart materials and structures, 21, 2012.

Nonlinear electromagnetic generators for wide band vibrational energy harvesting

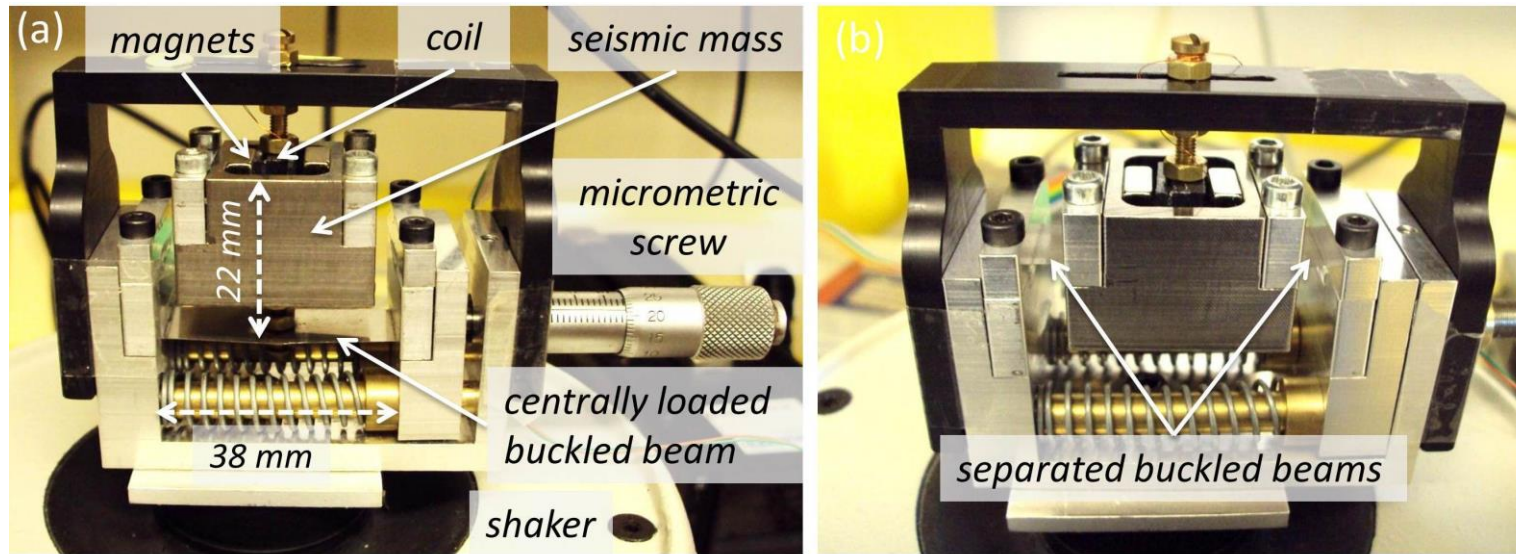


Figure 2. Photographs of the BEMG prototype for the (a) single centrally loaded-beam clamping configuration, (b) double-beam clamping configuration, and (c) scheme of the testing equipment.
 BEMG: beam electromagnetic generator; PC: personal computer; DAQ: data acquisition.

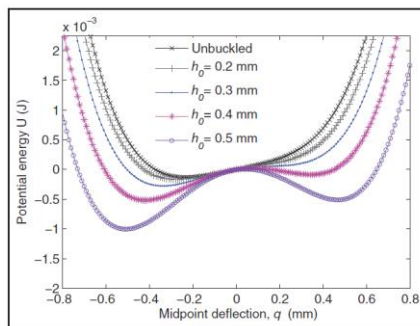


Figure 3. Potential energy of the system for increasing values of buckling height h_0 .

$$\frac{d^2 \tilde{q}(\tau)}{d\tau^2} + \frac{1}{Q} \frac{d\tilde{q}(\tau)}{d\tau} + \tilde{q}(\tau) + \tilde{q}^3(\tau) + \tilde{V}(\tau) = -\frac{d^2 \tilde{y}(\tau)}{d\tau^2},$$

$$\frac{d\tilde{V}(\tau)}{d\tau} + \frac{1}{\gamma} \tilde{V}(\tau) = k_{em}^2 \frac{d\tilde{q}}{d\tau},$$

$$\gamma = \omega_0 / (\omega_R + \omega_L)$$

$$k_{em}^2 = \frac{\lambda^2}{k_1 L_c} = \frac{(Bl)^2}{k_1 L_c}$$

$$k_{pz}^2 = \frac{\alpha^2}{k_1 C_0}$$

Nonlinear electromagnetic generators for wide band vibrational energy harvesting

Bandwidth enhancement of 2.5x with bistability at 0,2 grms

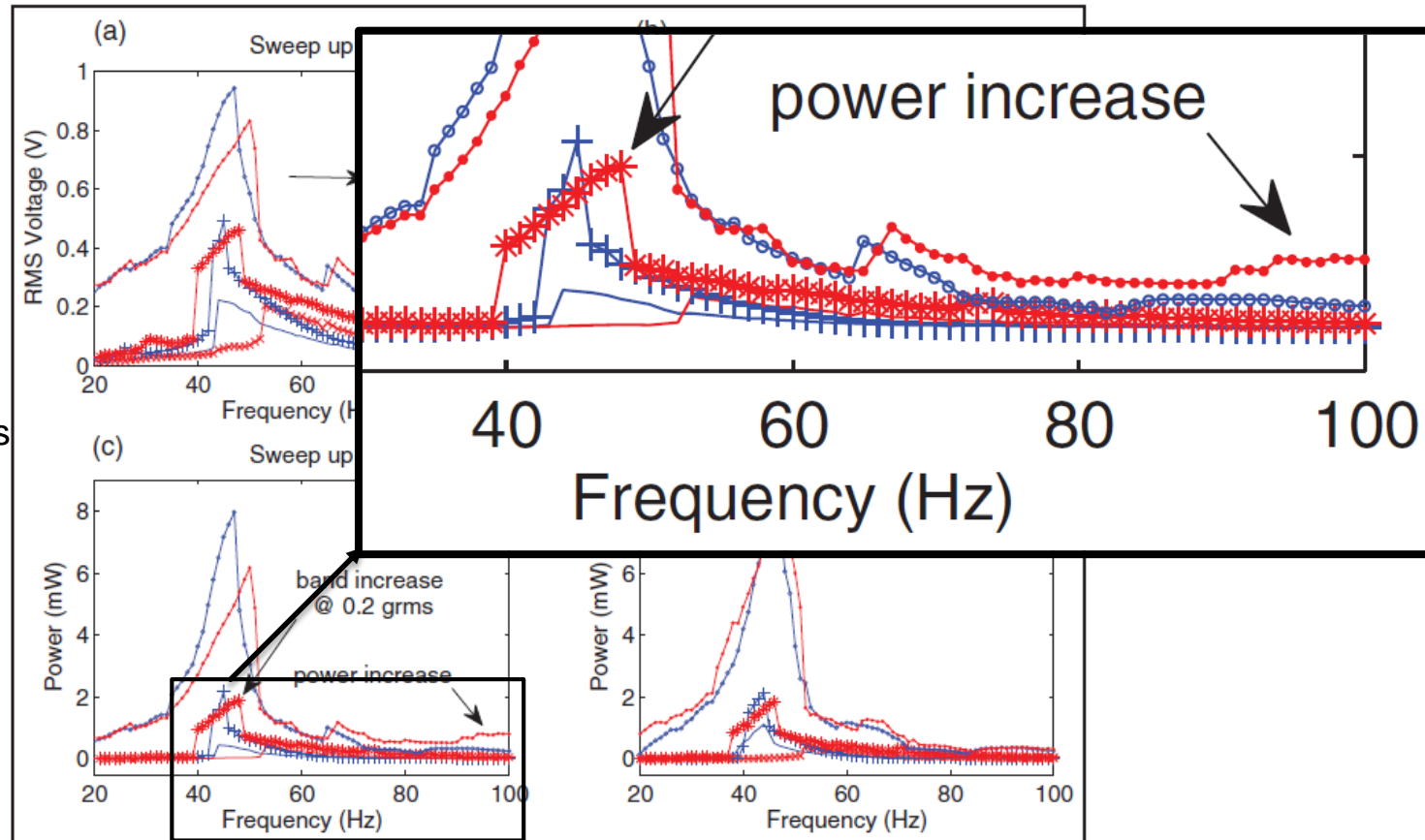
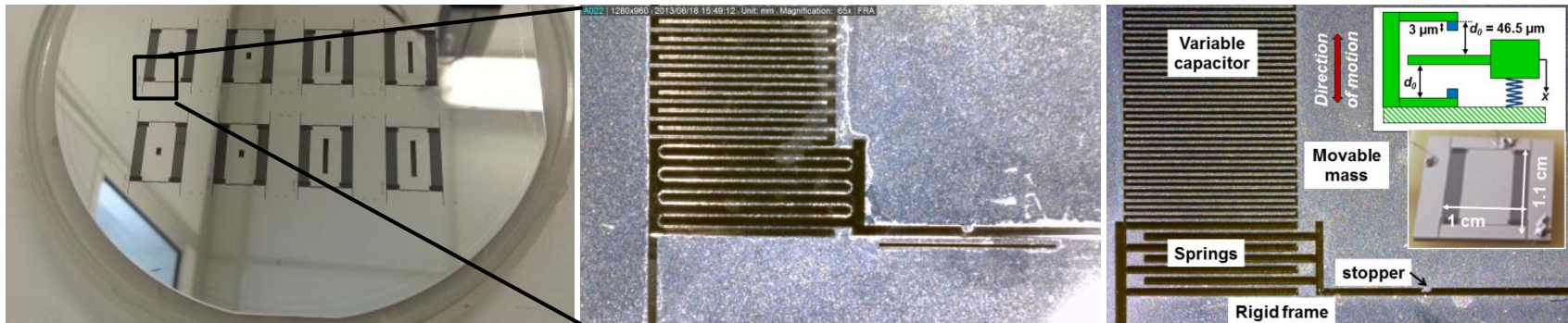


Figure 6. Experimental comparison of unbuckled- and buckled-beam ($h_0 = 0.3$ mm) generators for up (left column) and down (right column) frequency sweeps with acceleration amplitudes of 0.1, 0.2, and 0.5 g_{rms} . (a and b) rms voltage and (c and d) the corresponding power dissipated across the optimal load resistance $R_L = 112 \Omega$.

rms: root mean square.

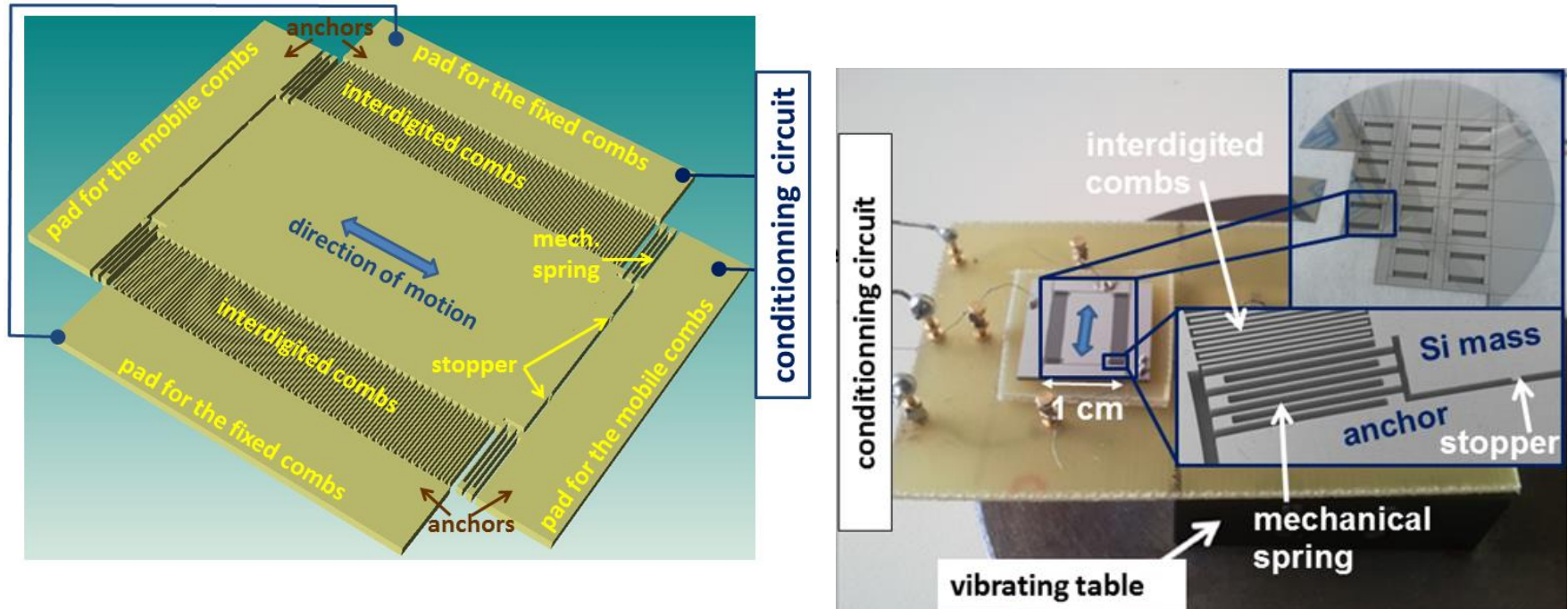
MEMS electrostatic kinetic energy harvester

Université Paris-Est, ESIEE Paris,
Silicon MEMS electrostatic harvesters.



- **Cottone, F.**, Basset, P., Guillemet, R., Galayko, D., Marty, F. and T. Bourouina. IEEE TRANSDUCERS 2013.
- R., Guillemet, Basset., P, Galayko, D., **Cottone, F.**, Marty, F. and T. Bourouina. Conf. Proceeding IEEE MEMS 2013.

MEMS electrostatic kinetic energy harvester



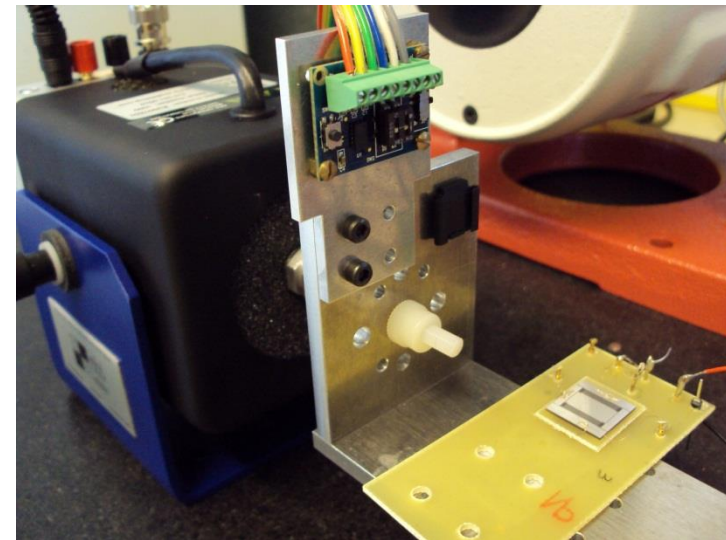
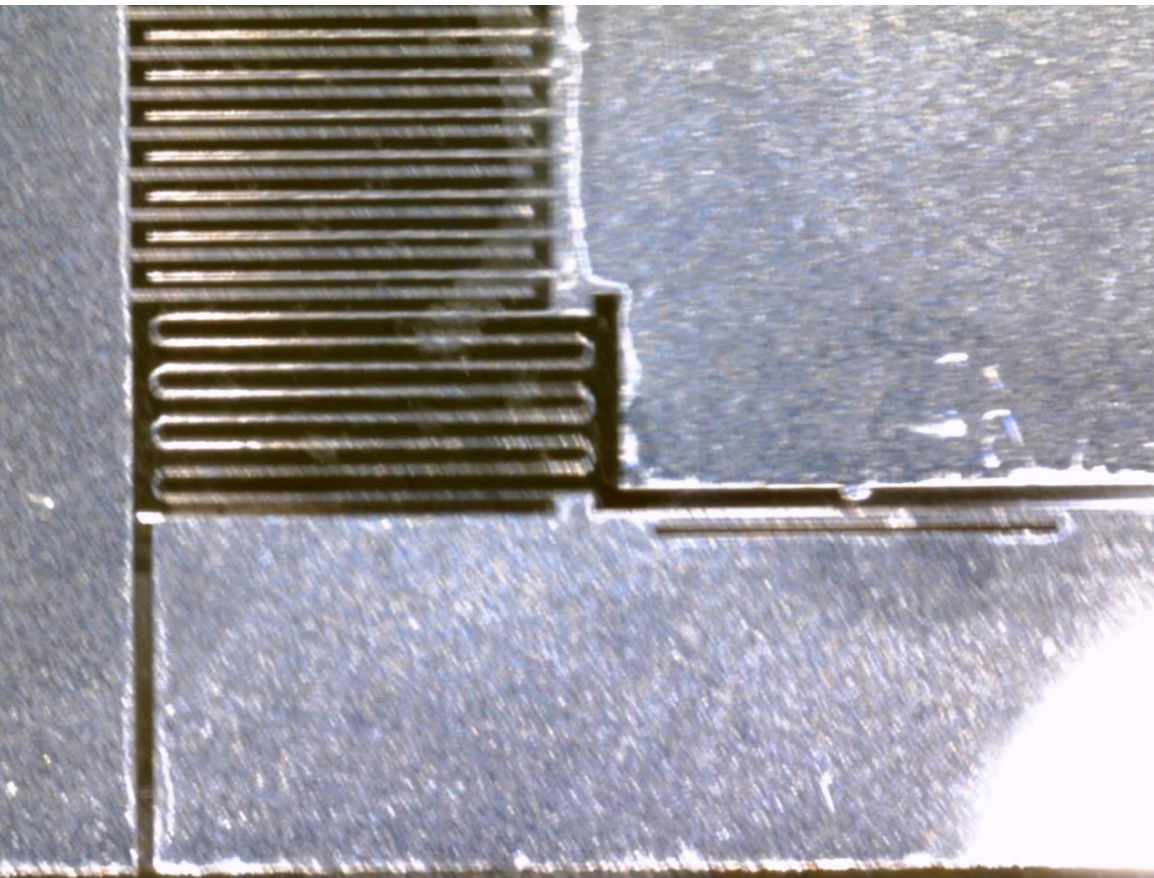
Guillemet, R., Basset, P., Galayko, D., Cottone, F., Marty, F., & Bourouina, T. (2013). *Micro Electro Mechanical Systems (MEMS), 2013 IEEE 26th International Conference on* (pp. 817-820): IEEE.

Cottone, F., Basset, P., Guillemet, R., Galayko, D., Marty, F., & Bourouina, T. (2013). *2013 Transducers & Eurosensors*.

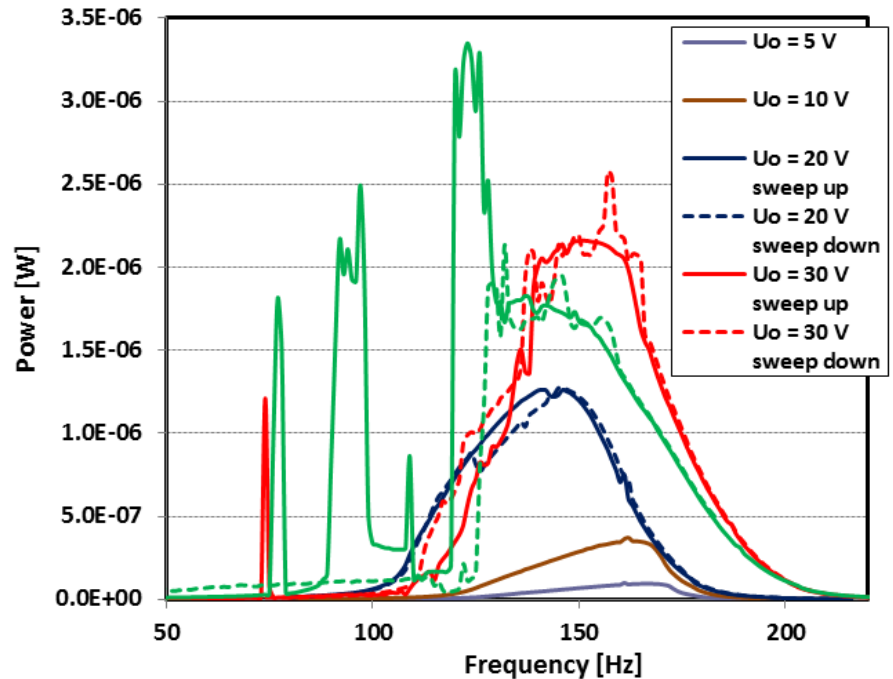
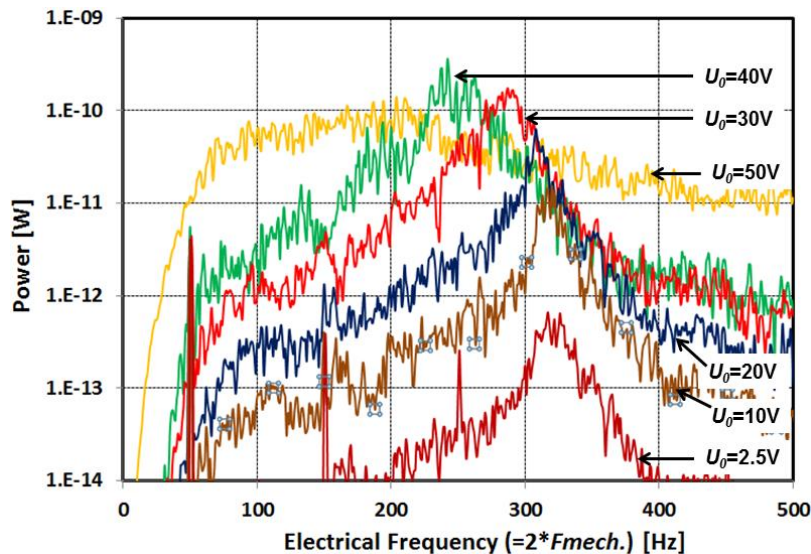
Basset, P., Galayko, D., Cottone, F., Guillemet, R., Blokhina, E., Marty, F., & Bourouina, T. (2014). *Journal of Micromechanics and Microengineering* 24(3), 035001

MEMS electrostatic kinetic energy harvester

F. Cottone, P. Basset Université Paris-Est, ESIEE Paris,
Silicon MEMS-based electrostatic harvesters.



MEMS electrostatic kinetic energy harvester



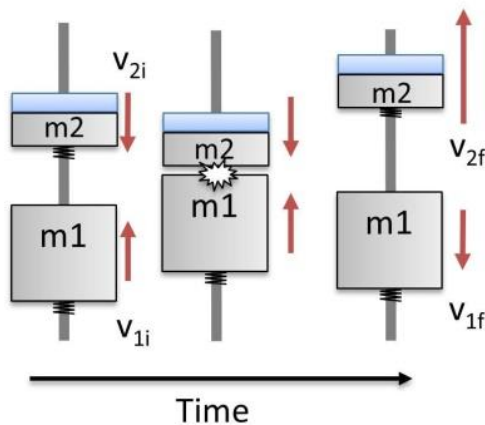
Cottone, F., Basset, P., Guillemet, R., Galayko, D., Marty, F., & Bourouina, T. (2013). *Transducers & Eurosensors*.

Basset, P., Galayko, D., Cottone, F., Guillemet, R., Blokhina, E., Marty, F., & Bourouina, T. (2014). *JMM* 24(3), 035001.

Electromagnetic generators

Velocity-amplified multiple-mass EM VEH

(a)



$$v_{2f} = \frac{(e+1)m_1 v_{1i} + (m_2 - em_1)v_{2i}}{m_1 + m_2}$$

if $e = 1$ and in the limit of $m_1 / m_2 \rightarrow \infty$,

the final velocity of the smaller mass is

$$v_{2f} = 2v_{1f} - v_{2i}$$

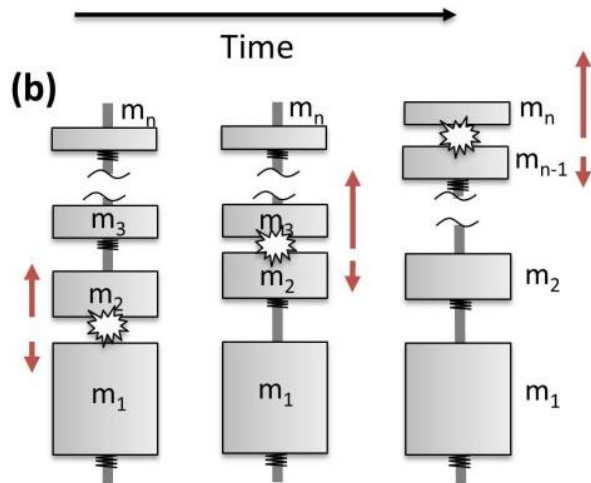
In the case of equal but opposite initial velocities

$$v_{2f} = -3v_{2i},$$

which represents a gain factor of **3x** in velocity.

Electromagnetic generators

Velocity-amplified multiple-mass EM VEH

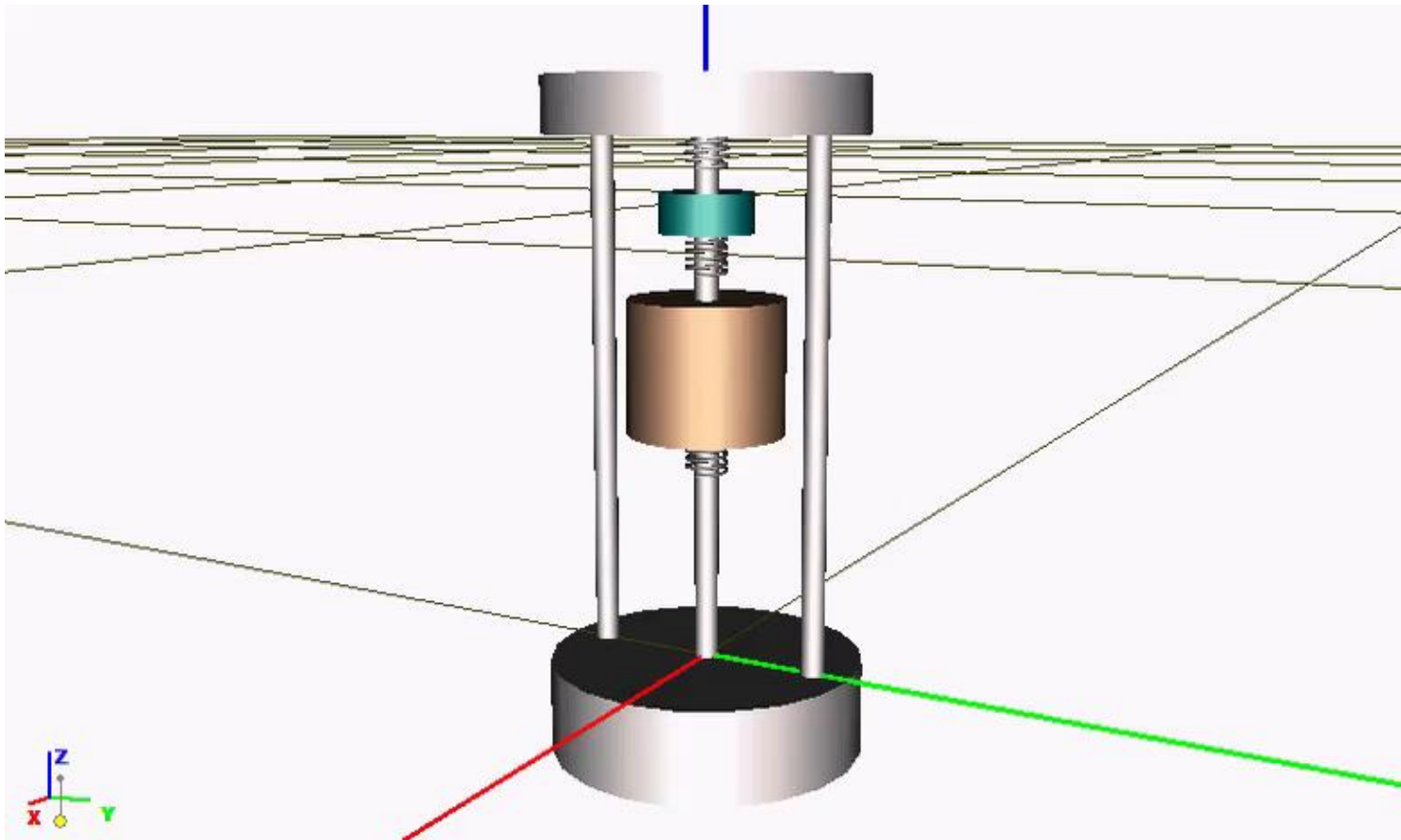


For a series of n -bodies of progressively smaller mass that impact sequentially, the velocity gain is proportional to n .
(Rodgers et al., 2008)

$$G_n = (1 + e_{1,0}) \prod_{k=2}^n \left(\frac{1 + e_{k,k-1}}{1 + r_{k,k-1}} \right) - 1$$

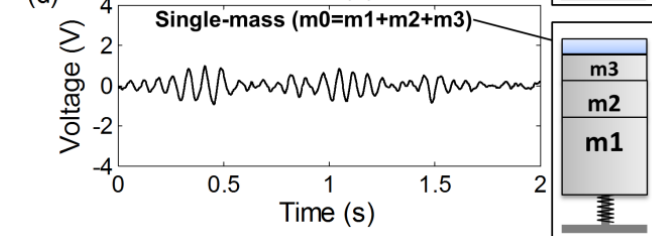
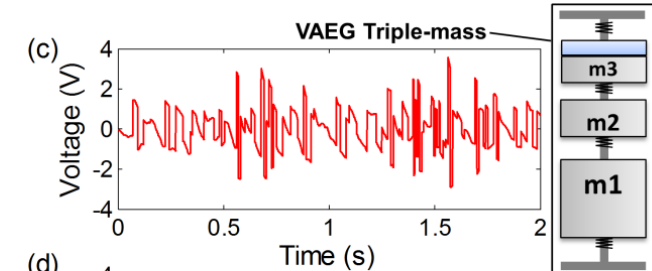
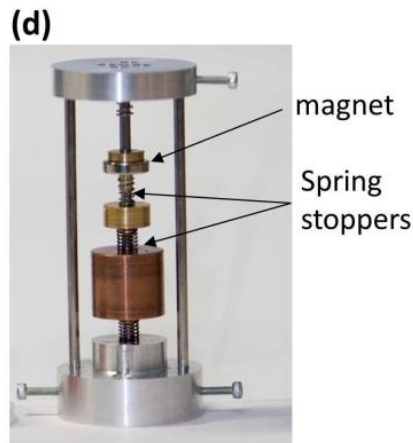
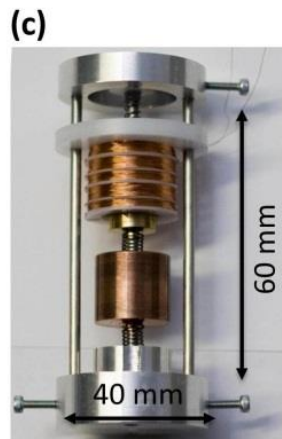
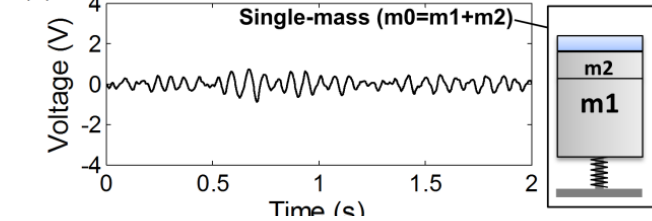
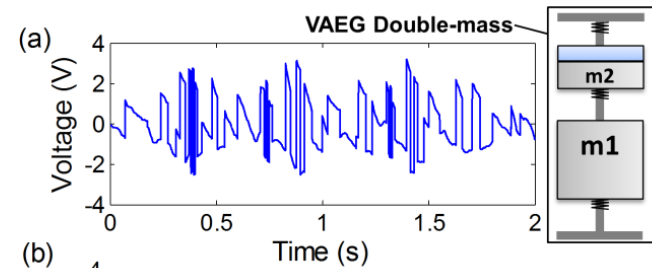
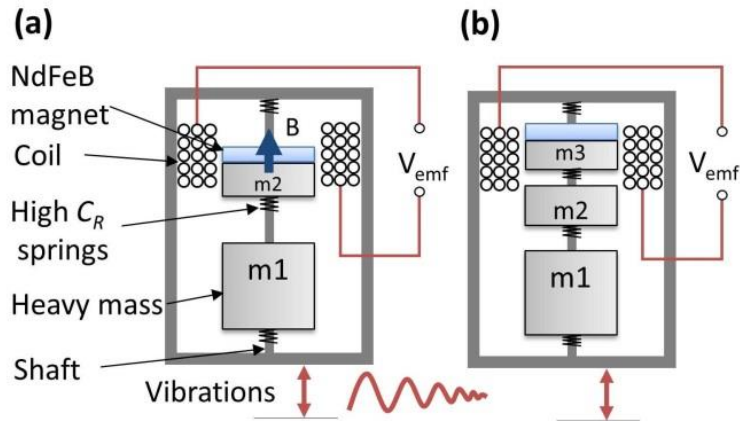
Electromagnetic generators

Velocity-amplified multiple-mass EM VEH



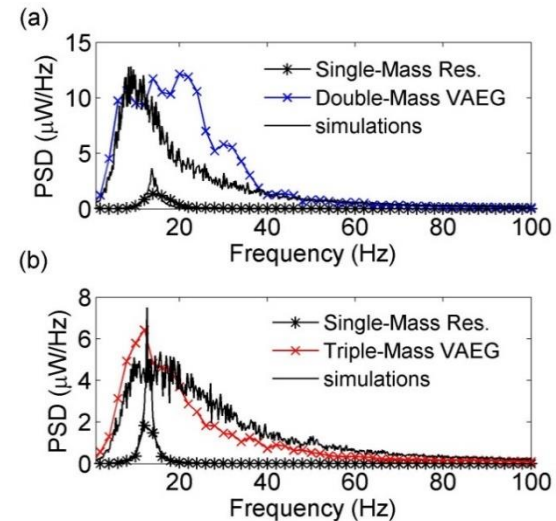
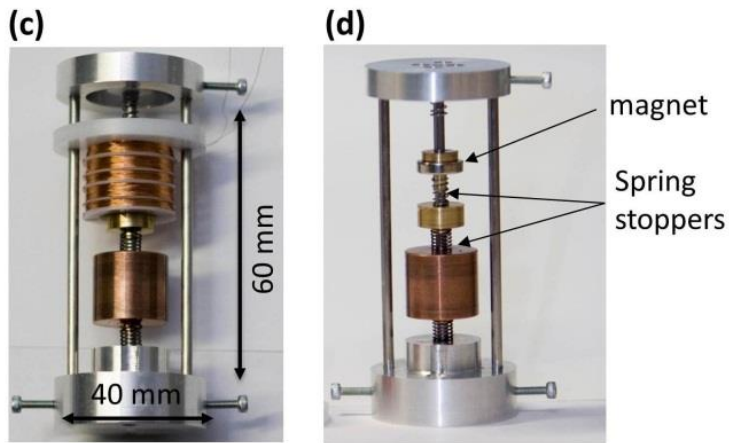
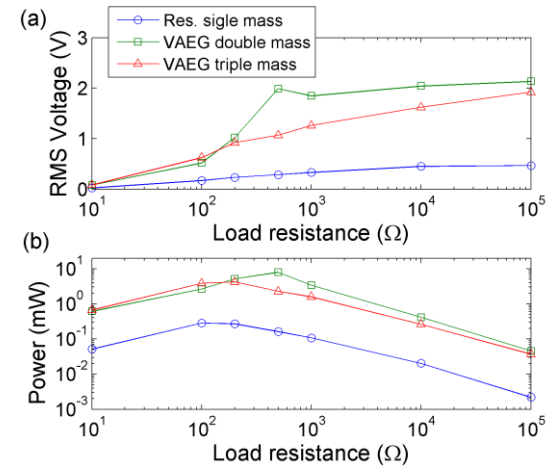
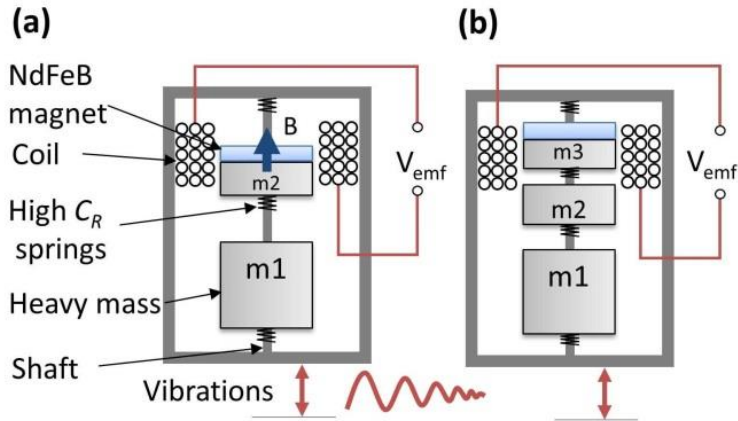
Electromagnetic generators

Velocity-amplified multiple-mass EM VEH



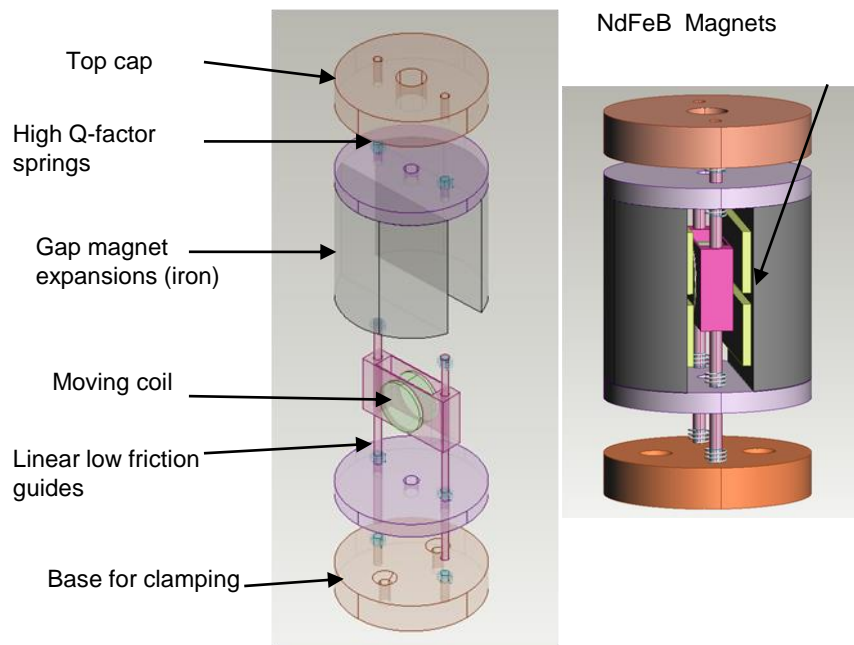
Electromagnetic generators

Velocity-amplified multiple-mass EM VEH

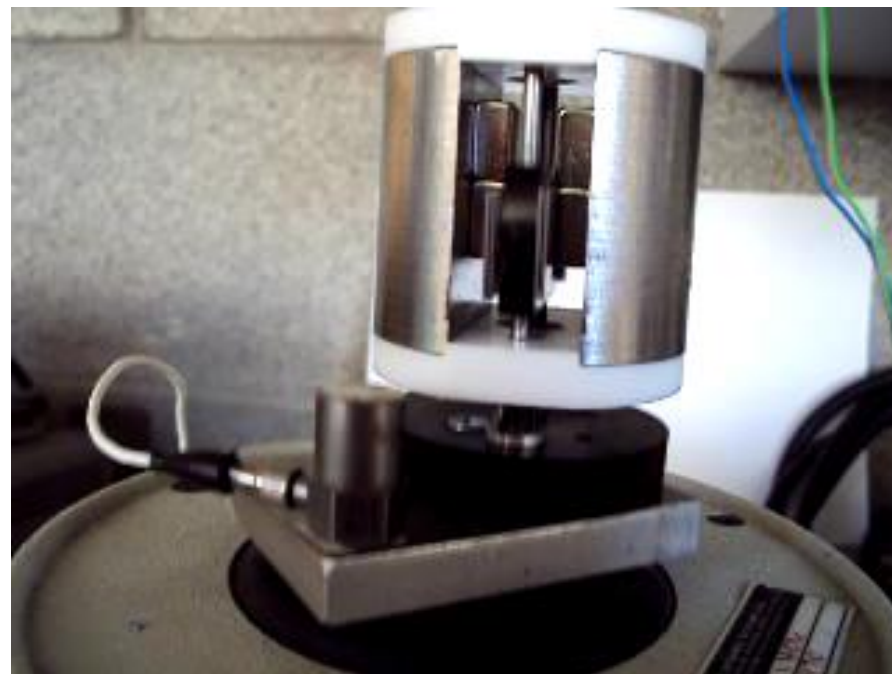


Electromagnetic generators

Velocity-amplified multiple-mass EM VEH



Prototype 2 with transversal magnetic flux

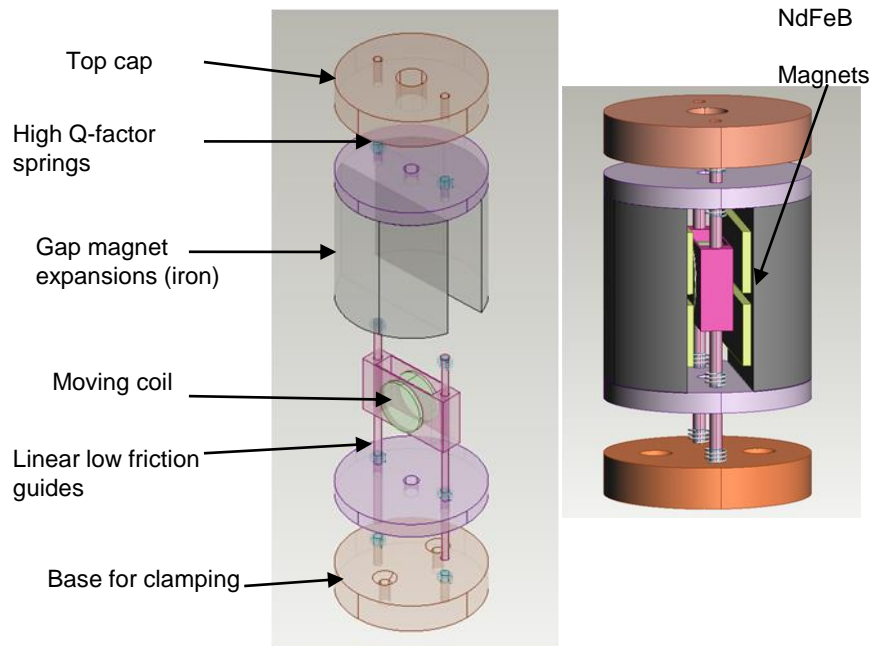


University of Limerick (Ireland) and Bell-Labs Alcatel (USA).

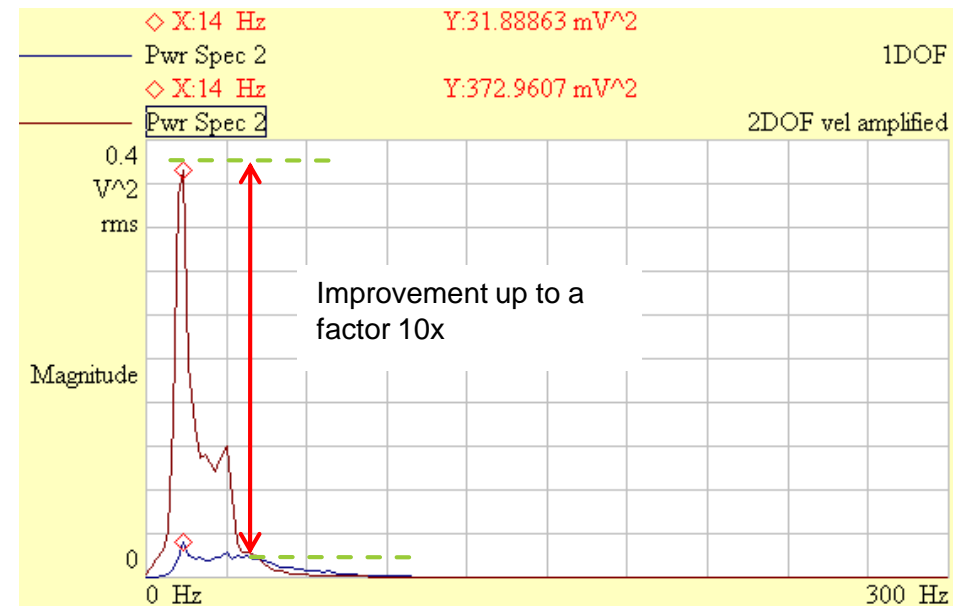
F. Cottone, G. Suresh, J. Punch - "Energy Harvesting Apparatus Having Improved Efficiency". US Patent n. 8350394B2

Electromagnetic generators

Velocity-amplified multiple-mass EM VEH



Prototype 2 with transversal flux linkage



University of Limerick (Ireland) and Bell-Labs Alcatel (USA).

F. Cottone, G. Suresh, J. Punch - "Energy Harvesting Apparatus Having Improved Efficiency". US Patent n. 8350394B2

Comparison of various approaches

Strategies	Advantages	Disadvantages
Mechanical tuning <ul style="list-style-type: none"> • Change dimension • Change centre of gravity • Change spring stiffness continuously • Apply axial load (change spring stiffness intermittently) 	<ul style="list-style-type: none"> • High efficiency • Does not affect damping • Does not affect damping • Suitable for <i>in situ</i> tuning • Easy to implement • Suitable for <i>in situ</i> tuning • No energy is required when generators work at resonance • Damping is not affected when the tensile load is applied 	<ul style="list-style-type: none"> • Extra system and energy are required • Responds to only one frequency at a time • Slow response to a change in a vibration frequency • Difficult to implement • Not suitable for tuning <i>in situ</i>^a • Not suitable for tuning <i>in situ</i> • Consumes energy when generators work at resonance • Increased damping when the compressive load is applied
Electrical tuning	<ul style="list-style-type: none"> • Easy to implement • No energy is required when generators work at resonance • Suitable for <i>in situ</i> tuning 	<ul style="list-style-type: none"> • Low tuning efficiency
Widen bandwidth <ul style="list-style-type: none"> • Generator array • Use mechanical stopper • Coupled oscillators • Nonlinear generators • Bi-stable structure 	<ul style="list-style-type: none"> • No tuning mechanism required • Respond to different frequencies at the same time • Immediate response to a change in vibration frequency • Damping is not affected • Easy to implement • Easy to implement • Better performance at excitation frequencies higher than resonant frequency • Better performance at excitation frequencies much lower than resonant frequency 	<ul style="list-style-type: none"> • Complexity in design • Complexity in design • Low volume efficiency • Fatigue problem • Decrease in the maximum output power • Decrease in the maximum output power • Complexity in design • Hysteresis • Complexity in design

^a Tuning while the generator is mounted on the vibration source and working. Zhu, D., Tudor, M. J., & Beeby, S. P. (2010).

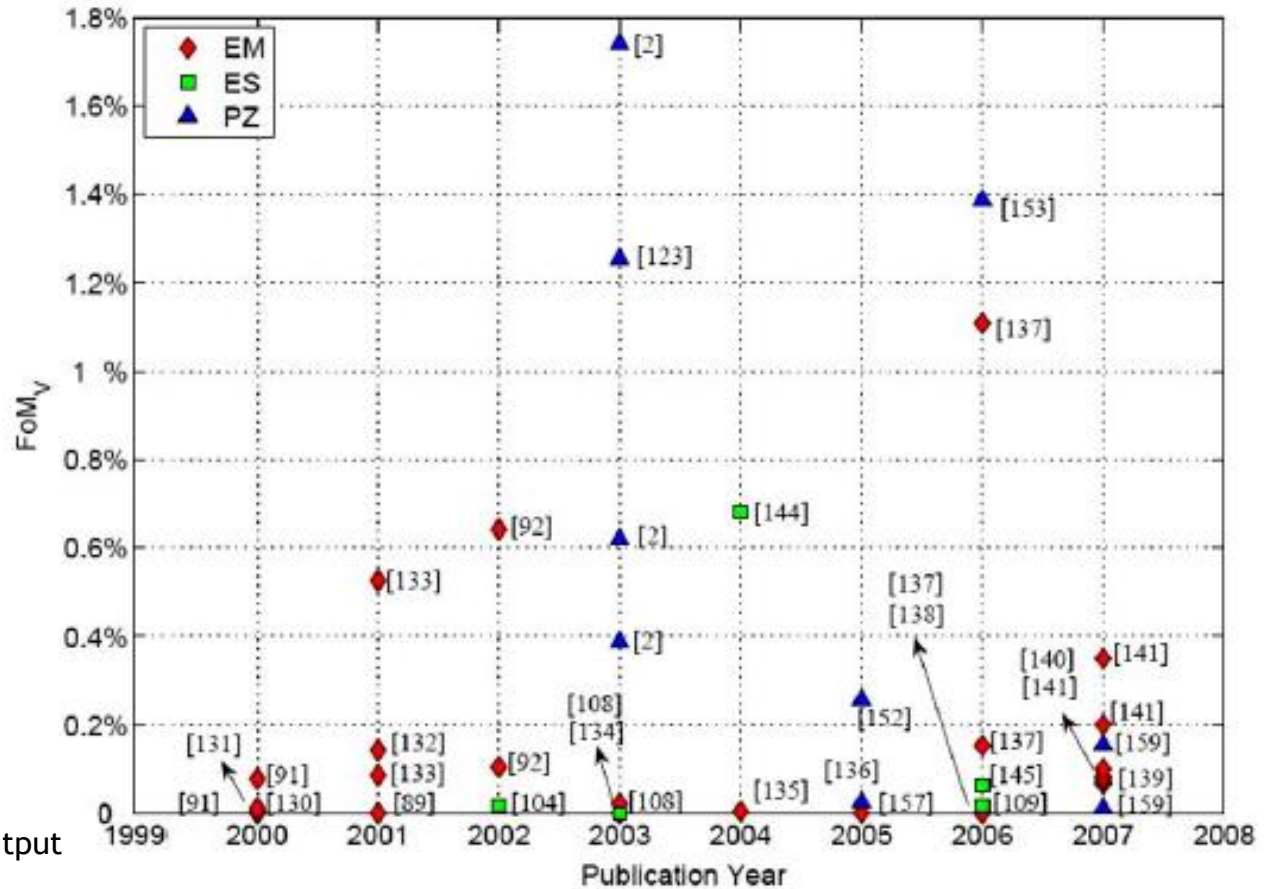
Performance metrics

$$FoM_V = \frac{\text{Useful Power Output}}{\frac{1}{16} Y_0 \rho_{Au} V_0 B^4 \omega^3}$$

Bandwidth figure of merit

$$FoM_{BW} = FoM_V \times \frac{\delta\omega_1 \text{ dB}}{\omega}$$

Frequency range within which the output power is less than 1 dB below its maximum value



Conclusions

- Marriage between Energy harvesting systems and Zero-power Technology will enable autonomous WSN applications
- Energy harvesting systems can be improved by:
 - Nonlinear dynamic: Bistable systems, frequency-up converters, impacting masses, electrostatic softening
 - Innovative electro-active materials (electrets, lead-free piezo)
 - Miniaturization
- Zero-Power Technology has plenty of room for improvement at level of
 - Low-consumption components,
 - Efficient conditioning.

Current technical challenges

- **Miniaturization issues**
 - Improvements of piezoelectric-material properties
 - Improving capacitive design
 - Increasing magnetic field in micro magnets
 - Research on electrets materials
- **Efficient conditioning electronics**
 - Efficient Integrated design
 - Power-aware operation of the powered device
- **Target applications**
 - Tailoring the WSN technology to specific applications

Acknowledgments

Thank you

